

# Hybrid Performance assessment of Sand Mitigation Measures

*VKI Seminar*

Lorenzo RAFFAELE

Politecnico di Torino

Department of Architecture and Design

von Karman Institute for Fluid Dynamics

Environmental and Applied Fluid Dynamics department

March 16<sup>th</sup>, 2022



**von KARMAN INSTITUTE  
FOR FLUID DYNAMICS**

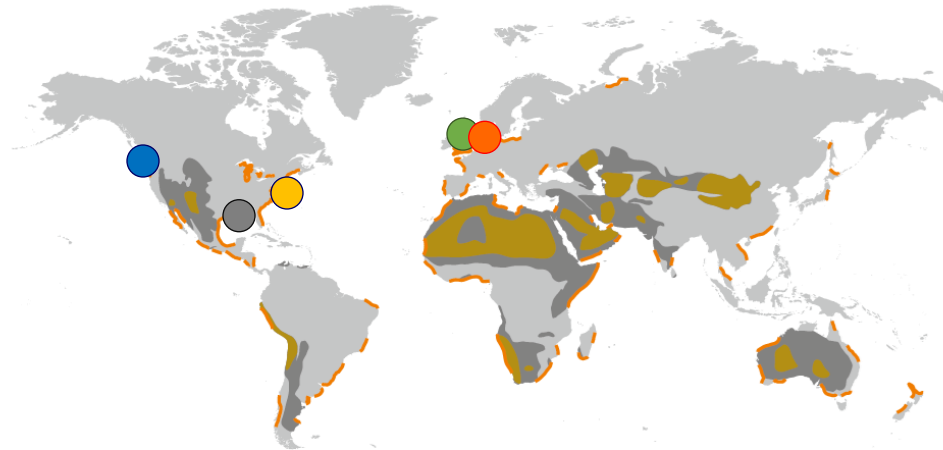


**Politecnico  
di Torino**



**OPTIFLOW**

# Industrial Motivation: coastal zones



- arid and desert regions
- active sand deposits
- coastal dunes

US



EU

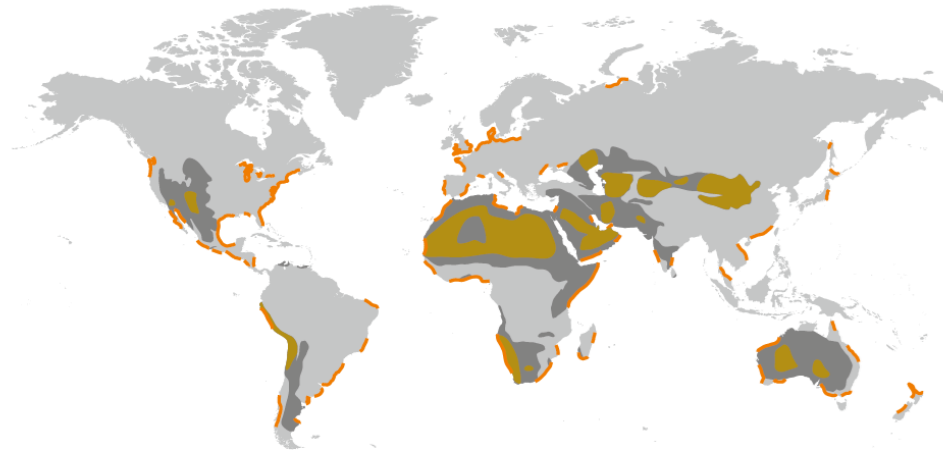


Windstorm frequency **+44%**

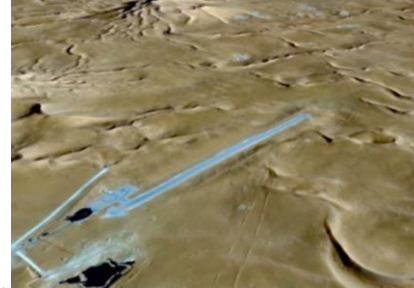
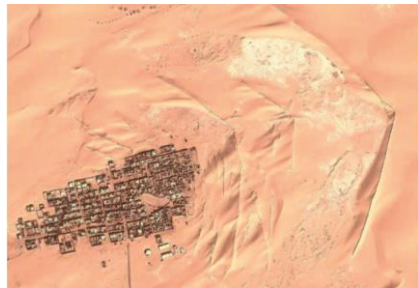
Windstorm intensity **+96%**



# Industrial Motivation: desert regions



- arid and desert regions
- active sand deposits
- coastal dunes



Structure scale

Urban scale

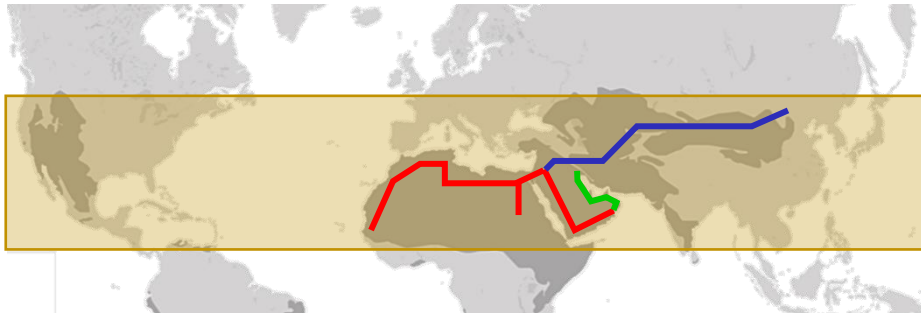
Infrastructure scale

# Industrial Motivation: railway megaprojects

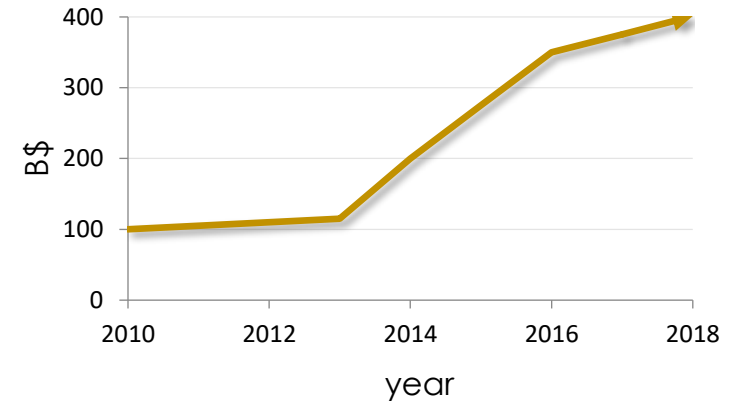


## Railway megaprojects

- Iron Silk Road
- Gulf Cooperation Council Network
- Arab League Network



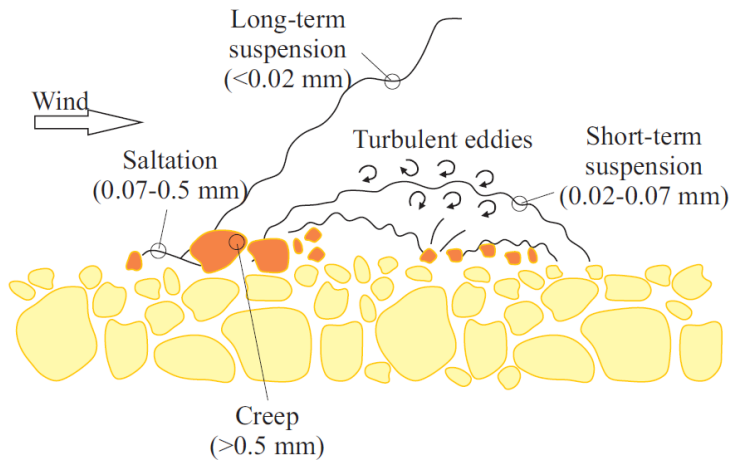
- arid regions
- northern desert belt



**Market potential      Railway length**

• **000** B\$      • **00000** Km

# Phenomenology

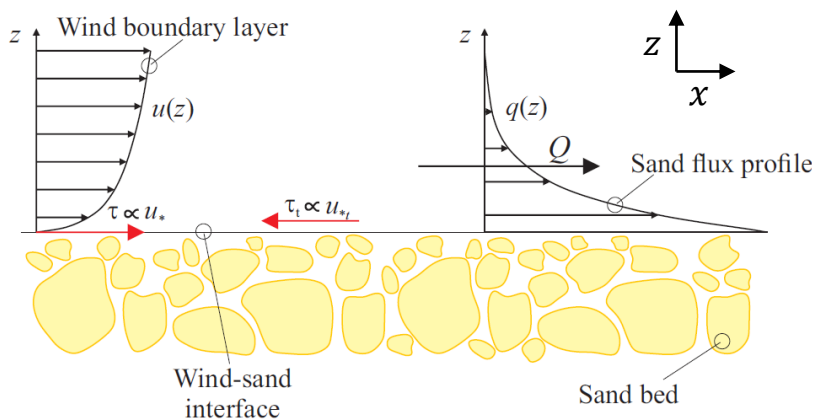


Dust  $d < 0.063$  mm • long-term suspension  
• short-term suspension

Sand  $d \in [0.063, 2]$  mm • creep  
• saltation

Engineering interest ↩

## Saltation



$$q(z) > 0 \iff \tau > \tau_t \quad \text{WbS saltation condition}$$

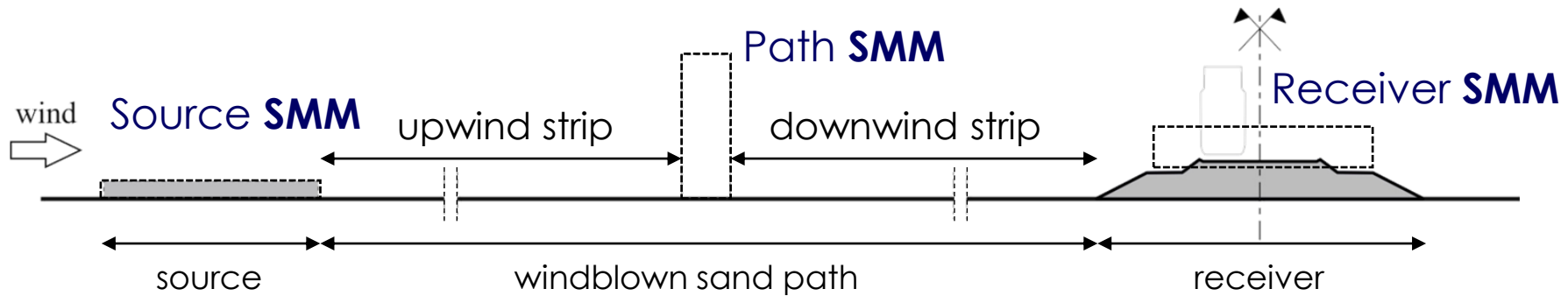
$$u_* = \sqrt{\tau / \rho_a} \quad u_* > u_{*t}$$

Threshold shear velocity

Sand transport rate  
[kg m<sup>-1</sup> s<sup>-1</sup>]

$$Q = \int_0^{+\infty} q(z) dz$$

# Sand Mitigation Measures: Source



from L. Bruno, M. Horvat, L. Raffaele (2018)

- Layer system



asphalt-latex mixture



natural crusting

$$Q \propto u_{*,eff} \propto \boxed{u_*^n} - \boxed{u_{*t}^n}$$

Hedge system
Layer system

- Hedge system



straw checkerboard



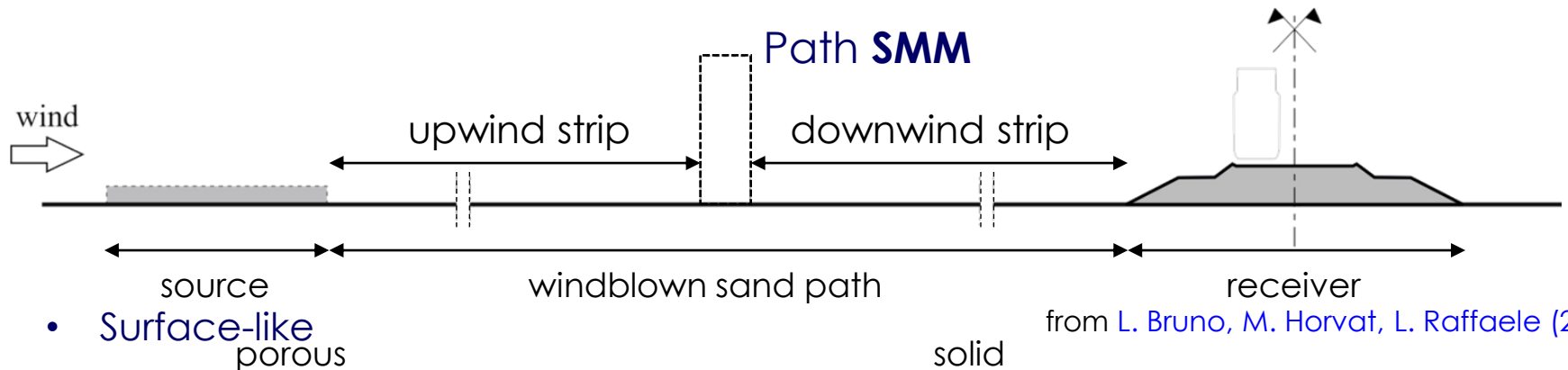
array line-like obstacles



gravel surface



# Sand Mitigation Measures: Path



- Surface-like porous

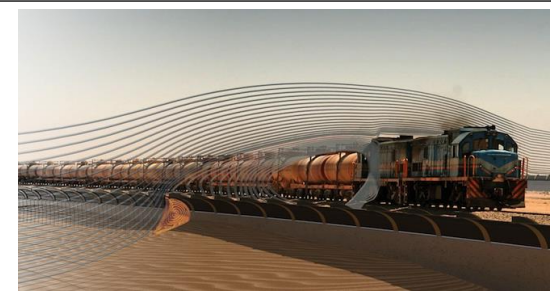


porous fence

- Volume-like



Straight Vertical Wall (SVW)



Shield for Sand (S4S)  
WO 2016/181417 A1

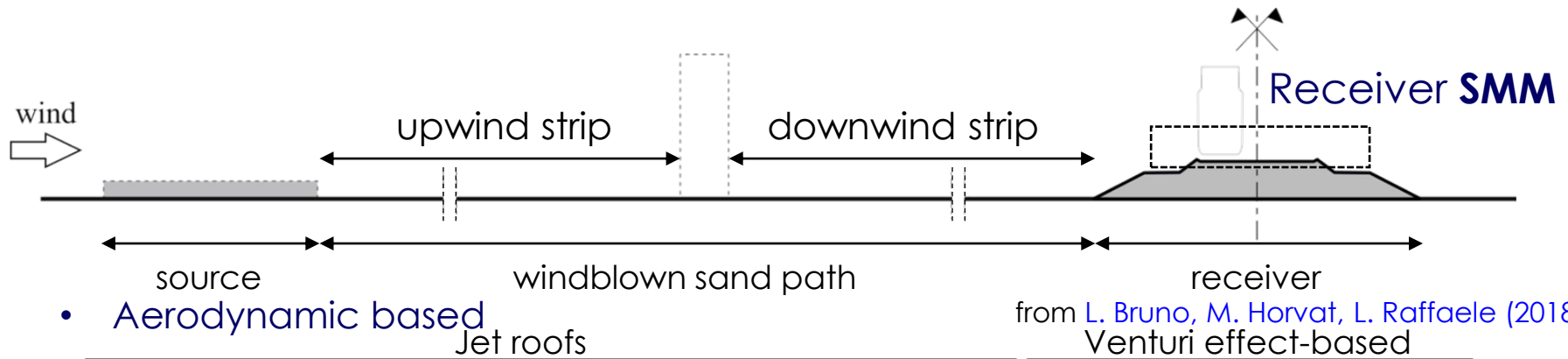


berm

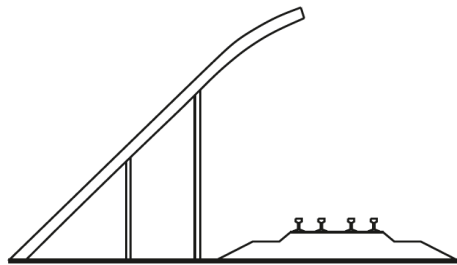


ditch

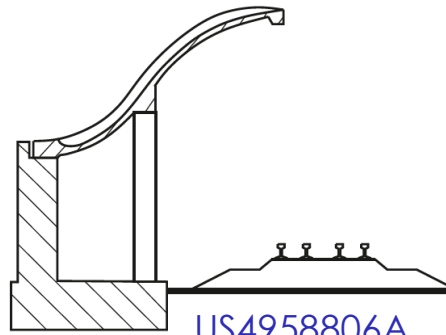
# Sand Mitigation Measures: Receiver



- Aerodynamic based



CN/102002916



US4958806A

- Sand-resistant



Humped sleepers



T-Track system



Continuous slab



Lubricant free turnout





## Hybrid Performance assessment of Sand Mitigation Measures



EU Horizon 2020 Marie Curie Individual Fellowship



von KÁRMÁN INSTITUTE  
FOR FLUID DYNAMICS



OPTIFLOW

WSMM

HyPer SMM received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 885985



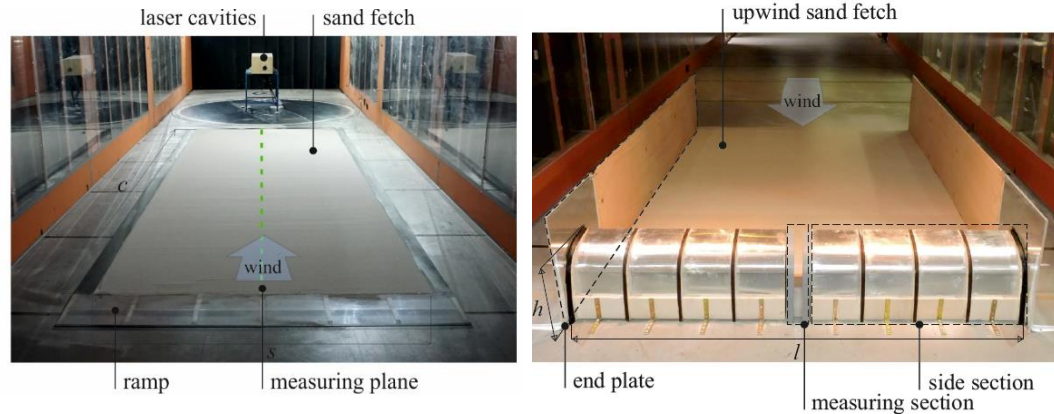
# HyPer SMM

- Aim

Develop an innovative **hybrid approach** by combining **Wind-Sand tunnel tests** and **Wind-Sand CFD** simulations as a brand-new design-and-assessment methodology in the field

- Main Tasks

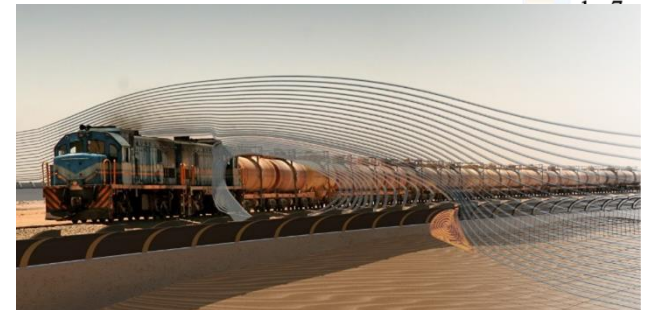
1. Development of highly reliable **Wind-Sand Tunnel Tests** to assess SMM performance (flat plane conditions + SMM obstacle)



2. Tuning and validation **Wind-Sand Eulerian multiphase CFD** model



3. Extrapolation of WSTT-based **performance from scale to full-scale** through Wind-Sand CFD simulations



# Windblown Sand Action: categorization

## Environmental

- site-dependent
- inborn randomness

## Free

- wind-dependent accumulation

## Variable

- long-term varying accumulation process
- non monotonic (periodic sand removal)

Windblown Sand



2 months later...



analogous to



~ wind



~ windblown snow



~ snow



~ / ≠ snow

modelling fallout

probabilistic modelling

Wind and sand modelling

Time-variant reliability analysis

Evaluation of sand removal period

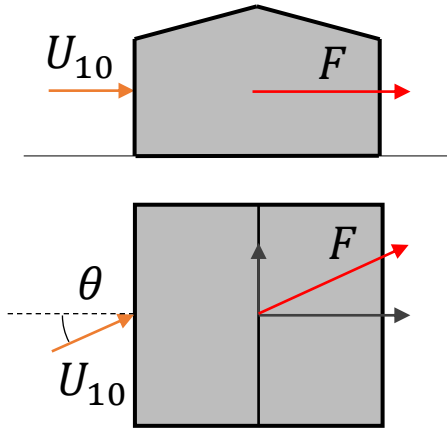
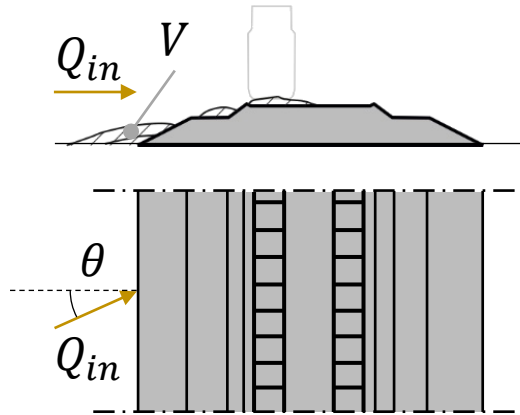


# Windblown Sand Action: modelling chain

## Windblown sand action

VS

## Wind action



Site  
analysis

1 Incoming  
Windblown Sand

•  $Q_{in}(U_{10}, d)$

Incoming Wind

•  $U_{10}$

Assessment

2 Aerodynamics /  
Morphodynamics

•  $C_s(\theta, \Gamma_0, V)$

aerodyn. morphodyn.

Aerodynamics

•  $C_f(\theta, \Gamma_0)$

3 Windblown sand  
action

•  $V \Rightarrow F \Rightarrow \dots$

Wind action

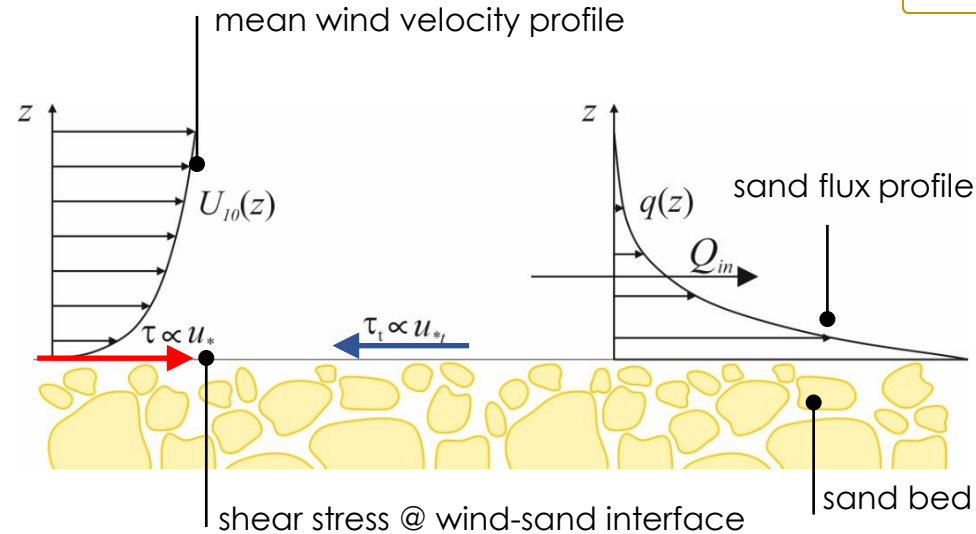
•  $F$

# Incoming Windblown Sand

1

2

3



## Semi-empirical models

- Bagnold type

$$Q \sim u_*^3$$

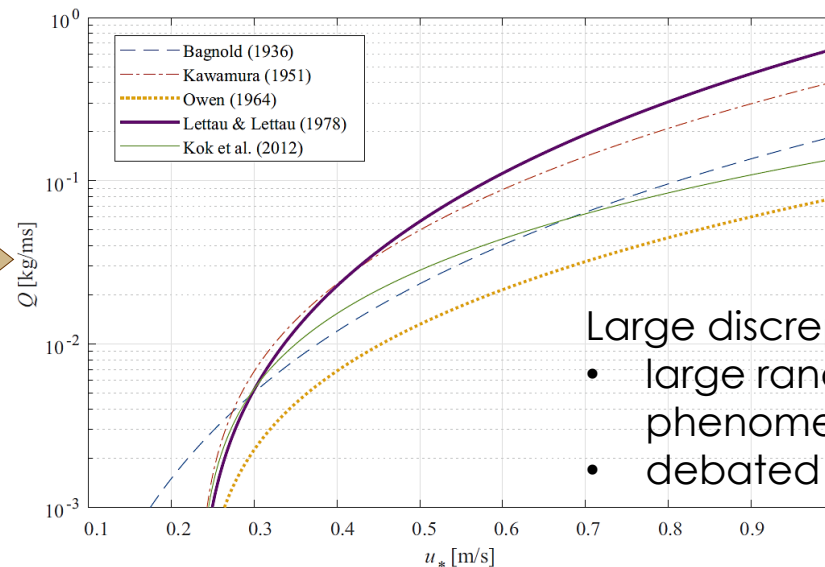
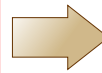
- Modified Bagnold type

$$Q \sim u_{*,eff}^3(u_*, u_{*t}), \omega_s$$

- O' Brien-Rindlaub type

$$Q \sim u$$

- Complex



Large discrepancies due to:

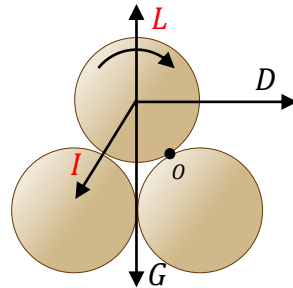
- large randomness of physical phenomenon
- debated scaling

# Modelling: $u_{*t}$

## Deterministic models

### Microscopic models

- Equilibrium of the moments
- Entraining aerodynamic forces VS
- Stabilizing forces



### Macroscopic models

- Semi-empirical (free parameters)
- Trend VS  $d$

$$u_{*t} = A \sqrt{\frac{\rho_p - \rho_a}{\rho_a} g d}$$

Bagnold (1941)

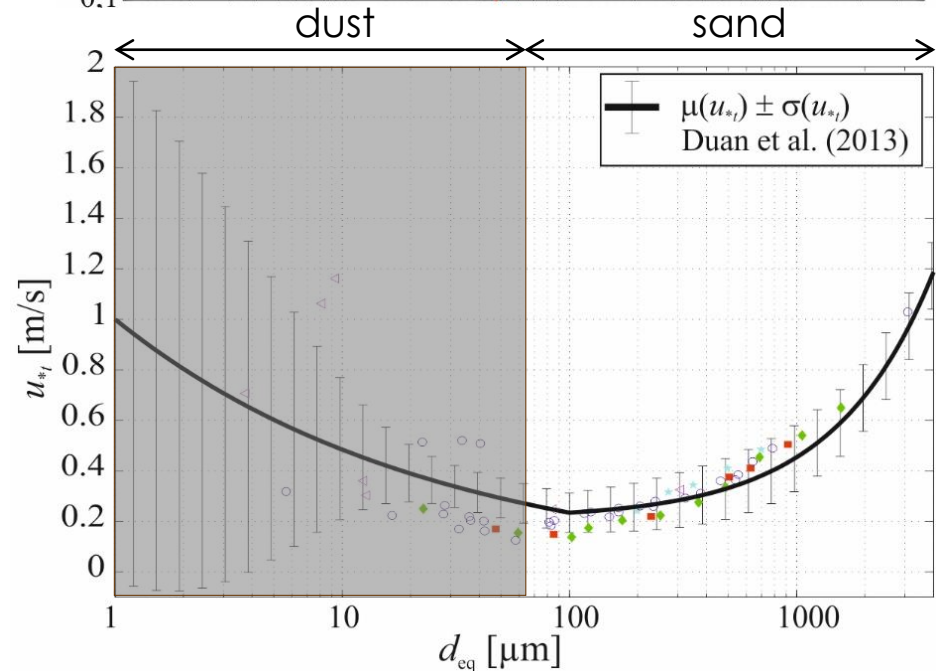
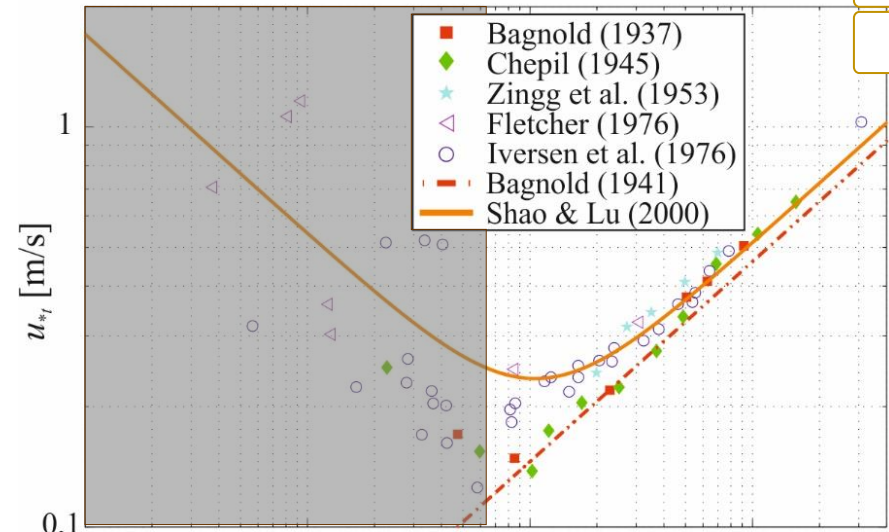
## Probabilistic models

- Scatter of experimental data
- Random turbulent wind flow, bed grain geometry, interparticle forces Zimon (1982)

Duan et al. (2013)

4 microscopic r.v.s

Modelling and technical difficulties





## Statistical approach

“Lack of exact knowledge, regardless of what is the cause of this deficiency” [Refsgaard et al. \(2007\)](#)



### Aleatory

- Sand uncertainties: grain size, shape, relative position, surface cleanliness, grain size distribution.
- Wind uncertainties: turbulent flow inborn variability, uncontrolled environmental conditions, e.g. temperature, humidity.

### Epistemic

- Model uncertainty: simplified representation of the real physical behaviour, identification of relevant variables, hypothesis, interactions left out. Lack of a shared definition of  $u_{*t}$  [Shao \(2008\)](#)
- Measurement uncertainty: errors and/or different procedures.
- Parameter uncertainty: values of model parameters.

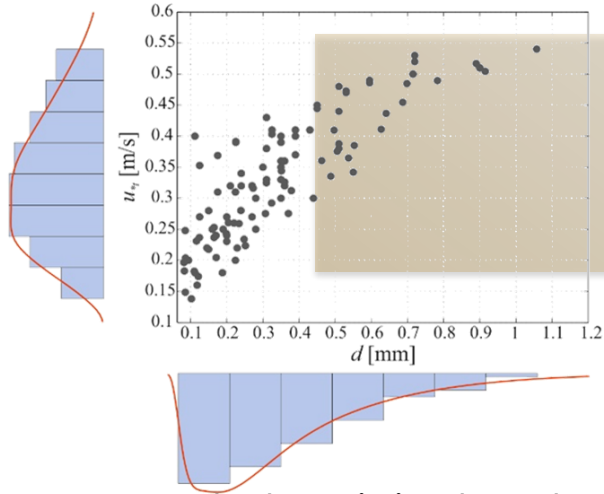


- Nonlinear regression
- Copula-based regression

# Modelling: $u_{*t}$

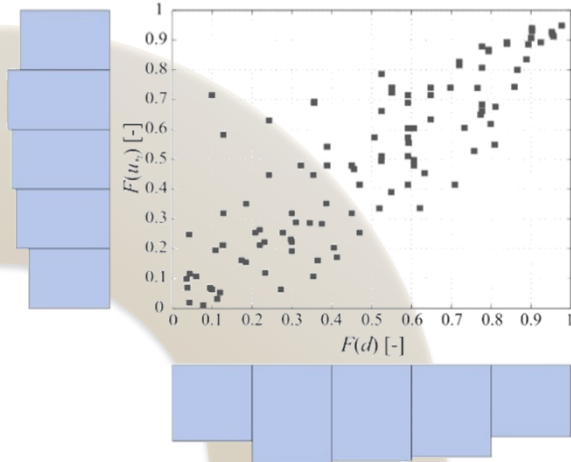
## 1 Fitting of marginal distributions

$$F(d), F(u_{*t}), \quad d, u_{*t} \in \mathbb{R}$$



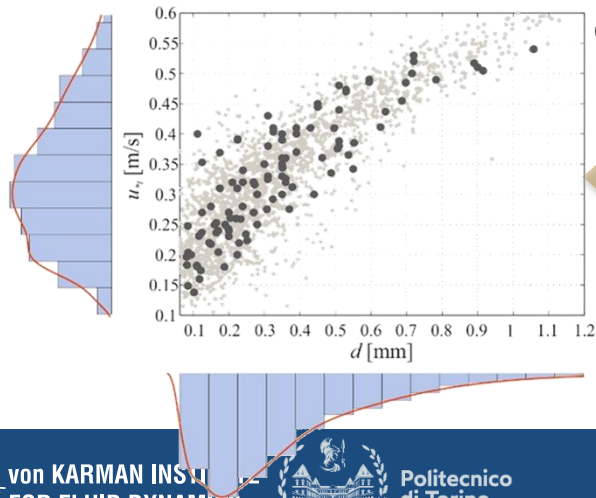
## 2 From original to copula scale

$$F(d, u_{*t}) = C\{F(d), F(u_{*t})\} \quad C: [0,1]^2 \rightarrow [0,1]$$



## 4 From copula to original scale

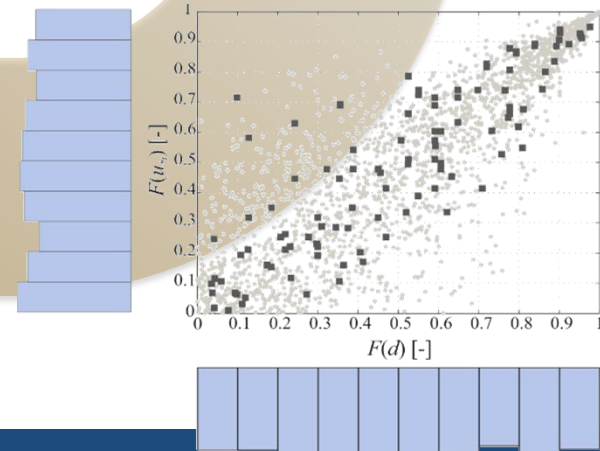
$$(d, u_{*t}) = (F^{-1}(u), F^{-1}(v))$$



## 3 Fitting of Inverted Clayton Copula

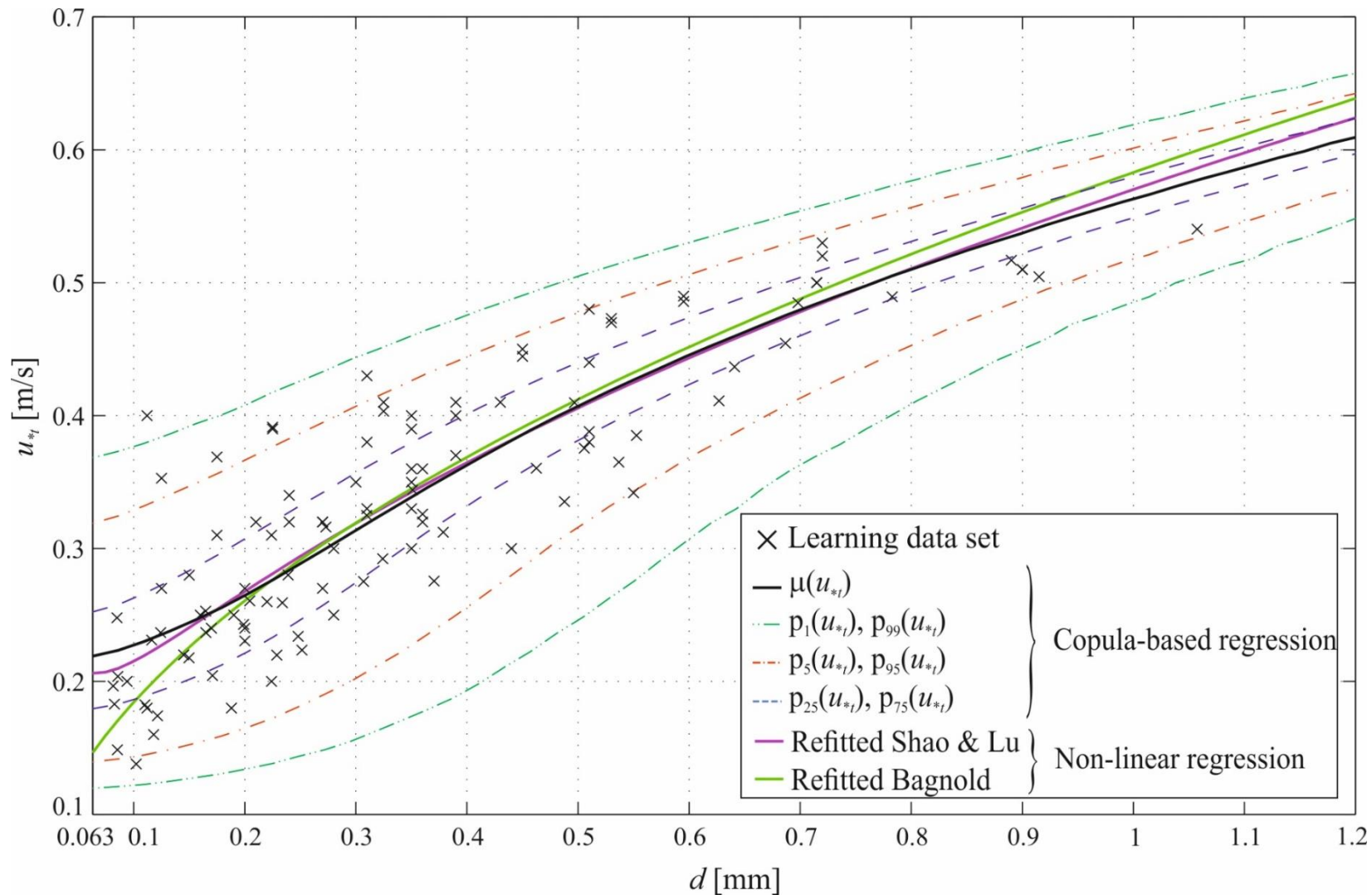
$$C(u, v) = u + v - 1 + [(1 - u)^{-1/\alpha} + (1 - v)^{-1/\alpha} - 1]^{-\alpha}$$

$$u, v \in [0,1], \alpha > 0$$



# Modelling: $u_{*t}$

1  
2  
3

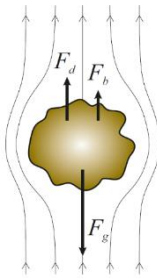


from L. Raffaele, L. Bruno, F. Pellerrey, L. Preziosi (2016)



## Statistical approach

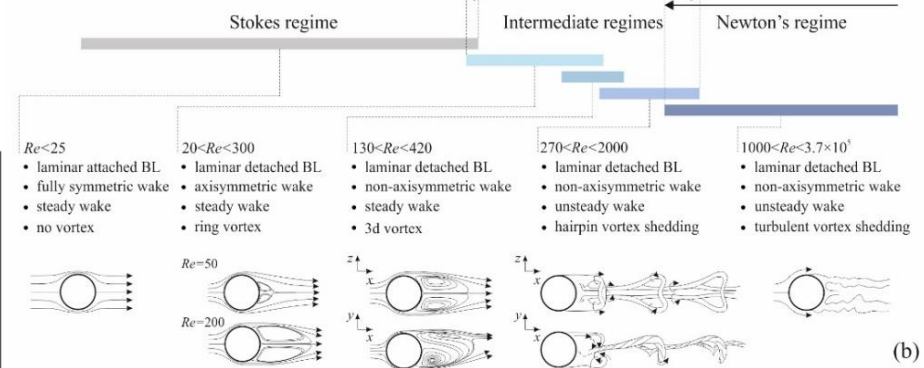
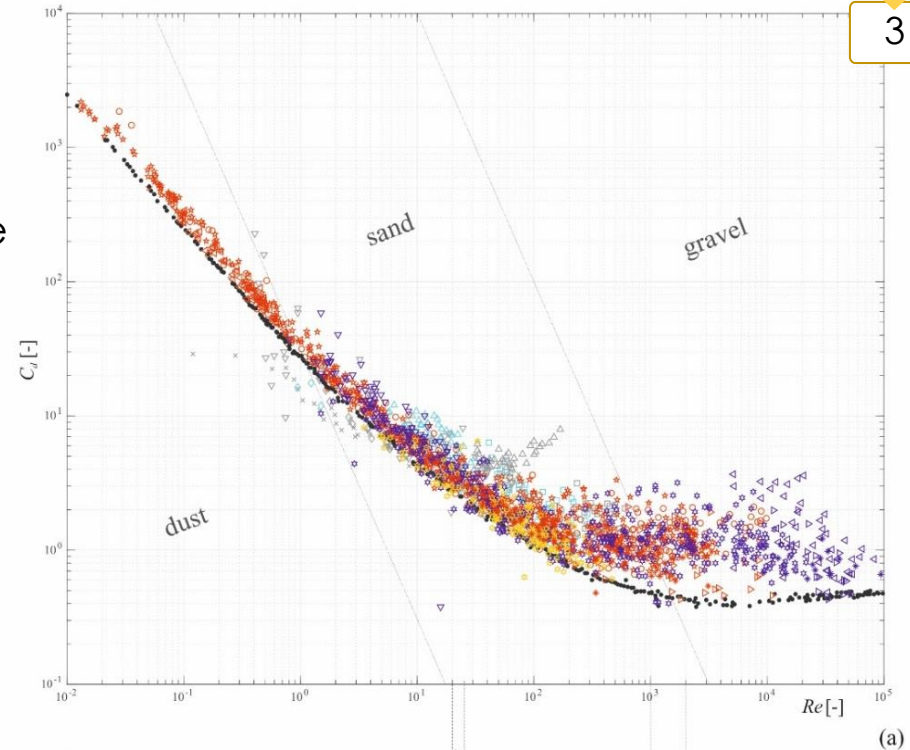
- Sedimentation velocity affects the mode of transport, distribution of particles above the ground, and transport rate
- Discrepancy among semi-empirical laws
- Sedimentation velocity bound to drag coefficient



$$F_d = \frac{1}{2} \rho_f \omega_s^2 C_d \frac{\pi d^2}{4}$$

$$F_g = \rho_p g \frac{\pi d^3}{6}$$

$$F_b = \rho_f g \frac{\pi d^3}{6}$$

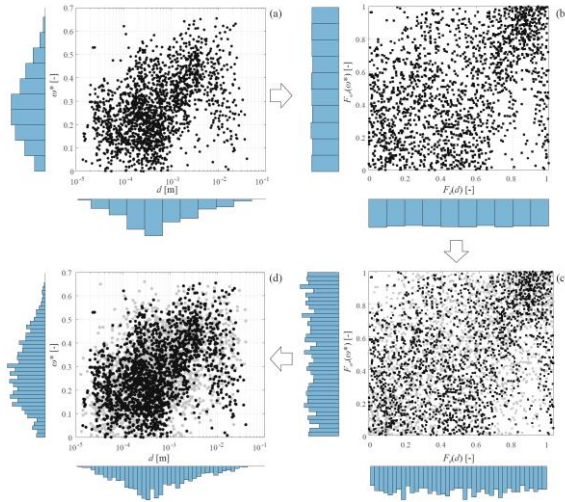


from [L. Raffaele, L. Bruno, D. Sherman \(2020\)](#)

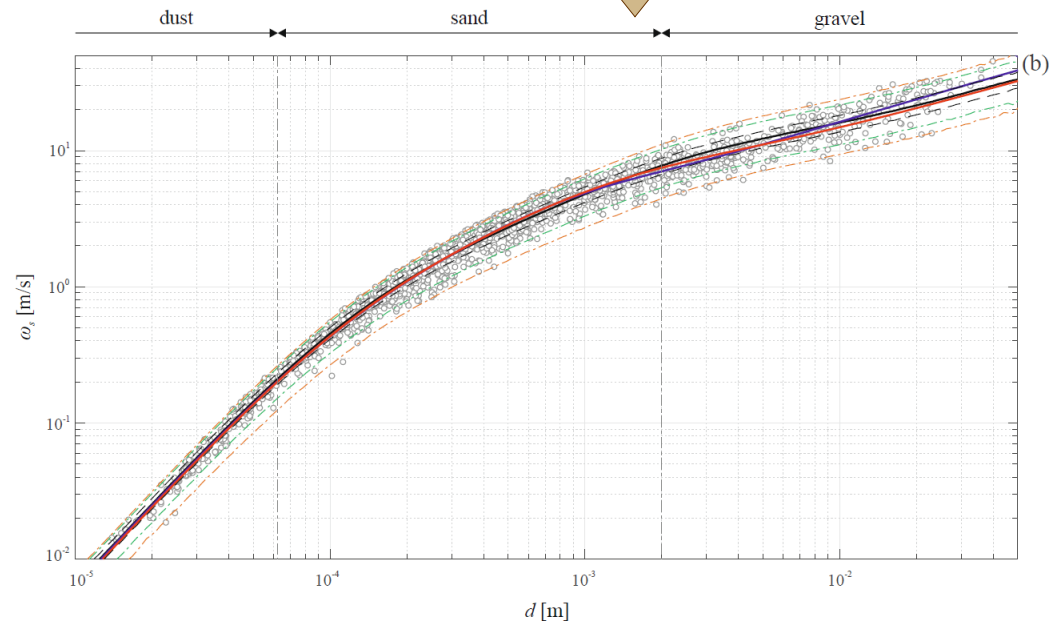
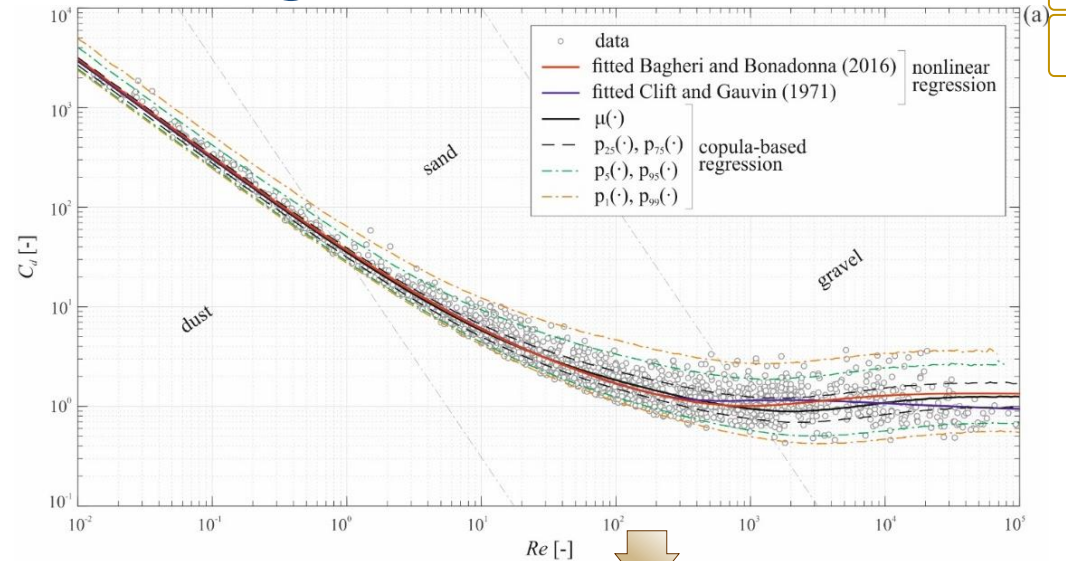
● smooth spheres for reference (Brown and Lawler, 2003)													
air	water	glycerine	oil	discarded		air	water	glycerine	discarded		glycerine	discarded	
△				△	Bagnold (1935)		✱	✱	✱	Stringham et al. (1969)	×	Chen and Fryrear (2001)	
✱		✱	✱	✱	Schultz (1954)		△	△		Komar and Reimers (1978)	○	○	Dioguardi et al. (2017)
▽				▽	Briggs et al. (1962)				▽	Wilson and Huang (1979)	★	★	Wang et al. (2018)
▽	△			▽	Alger (1964)		□		□	Cui et al. (1983)			
△				△	Romanovskiy (1966)		◇		◇	Malcolm and Raupach (1991)			

# Modelling: $\omega_s$

## copula-based regression



$$\left\{ \begin{array}{l} Re = \frac{\omega_s d}{\nu_f} \\ C_d = \frac{4 \rho_f (\rho_p - \rho_f)}{3 Re^2 \mu_f^2} g d^3 \end{array} \right. \quad \longleftrightarrow \quad \left\{ \begin{array}{l} d = \left[ \frac{3 C_d Re^2 \mu_f^2}{4 \rho_f (\rho_p - \rho_f) g} \right]^{1/3} \\ \omega_s = \frac{Re \nu_f}{d} \end{array} \right.$$

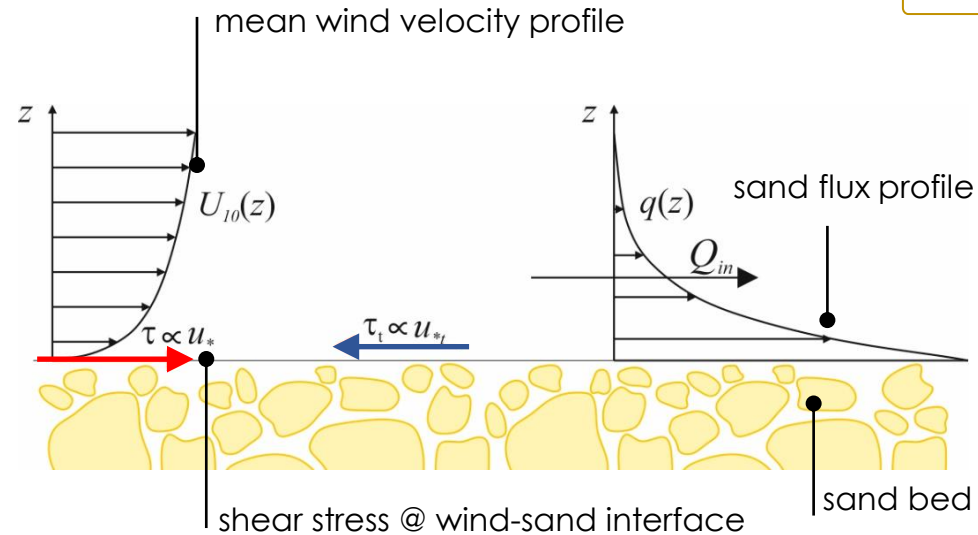


# Incoming Windblown Sand

1

2

3



Wind shear velocity

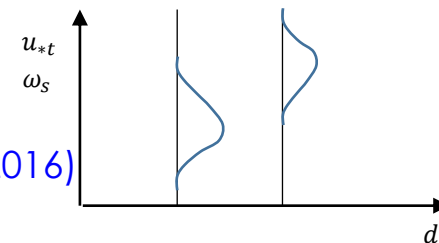
$$u_* = u_*(U_{10}, z_0)$$

$$f(u_*) = \frac{kf(U_{10,ref})}{\ln z_{ref}/z_0}$$

Threshold shear velocity

$$u_{*t} \approx u_{*t}(d)$$

$$f(u_{*t}|d) \text{ from Raffaele et al (2016)}$$



Sedimentation velocity

$$\omega_s \approx \omega_s(d)$$

$$f(\omega_s|d) \text{ from Raffaele et al (2020)}$$

Incoming sand transport rate

$$Q_{in} = \int_0^{+\infty} q(z) dz$$

$$\approx Q_{in}(u_*, u_{*t}, \omega_s)$$

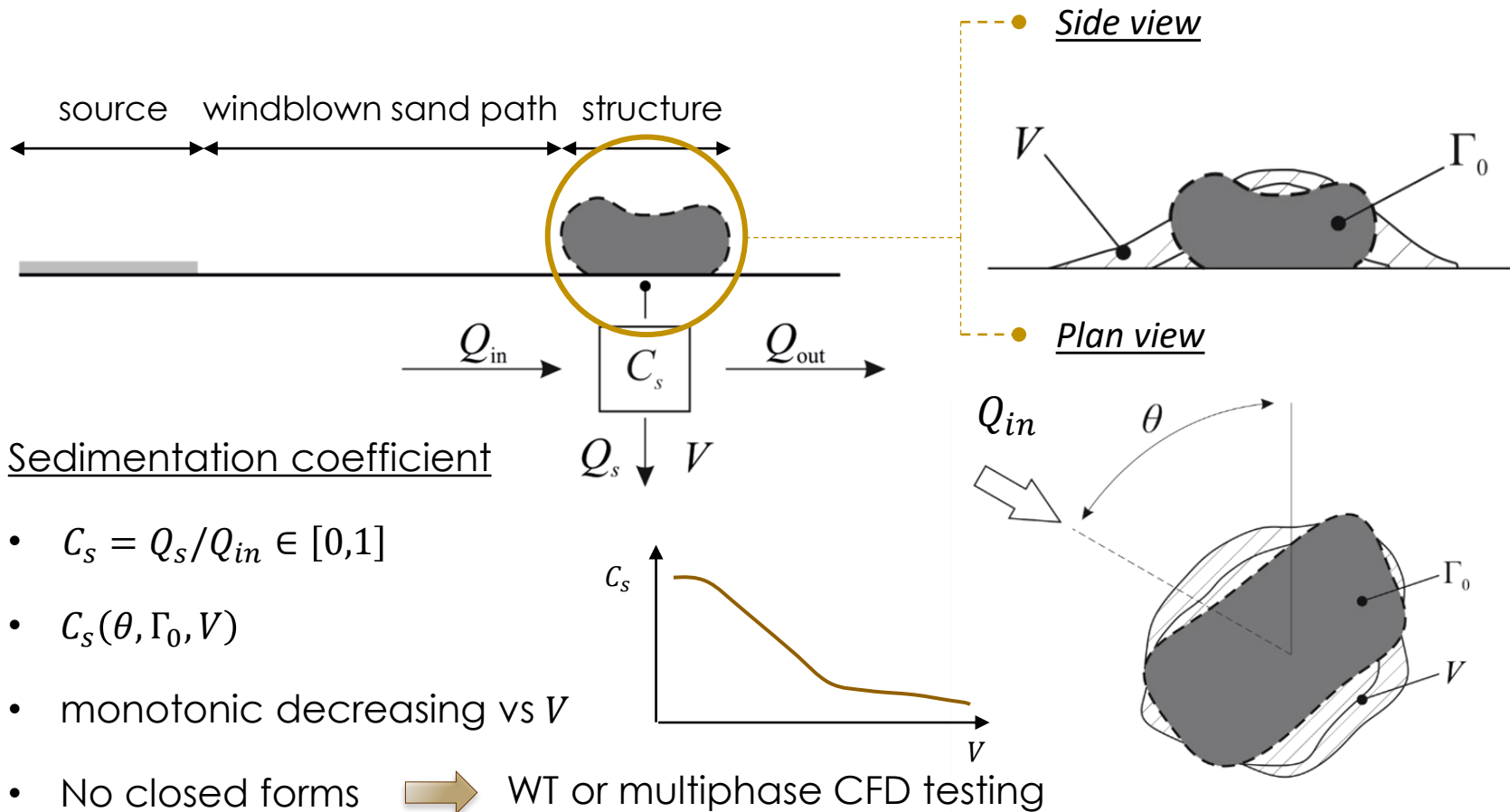
$$f(Q_{in}) = \begin{cases} A \sqrt{\frac{d}{d_r}} \frac{\rho_a}{g} f(u_*)^3 \left[ 1 - \frac{f(u_{*t}|d)}{f(u_*)} \right] & \text{if } u_* > u_{*t} \\ 0 & \text{if } u_* \leq u_{*t} \end{cases}$$

from Raffaele et al (2017a)



# Aerodynamics/Morphodynamics

1  
2  
3

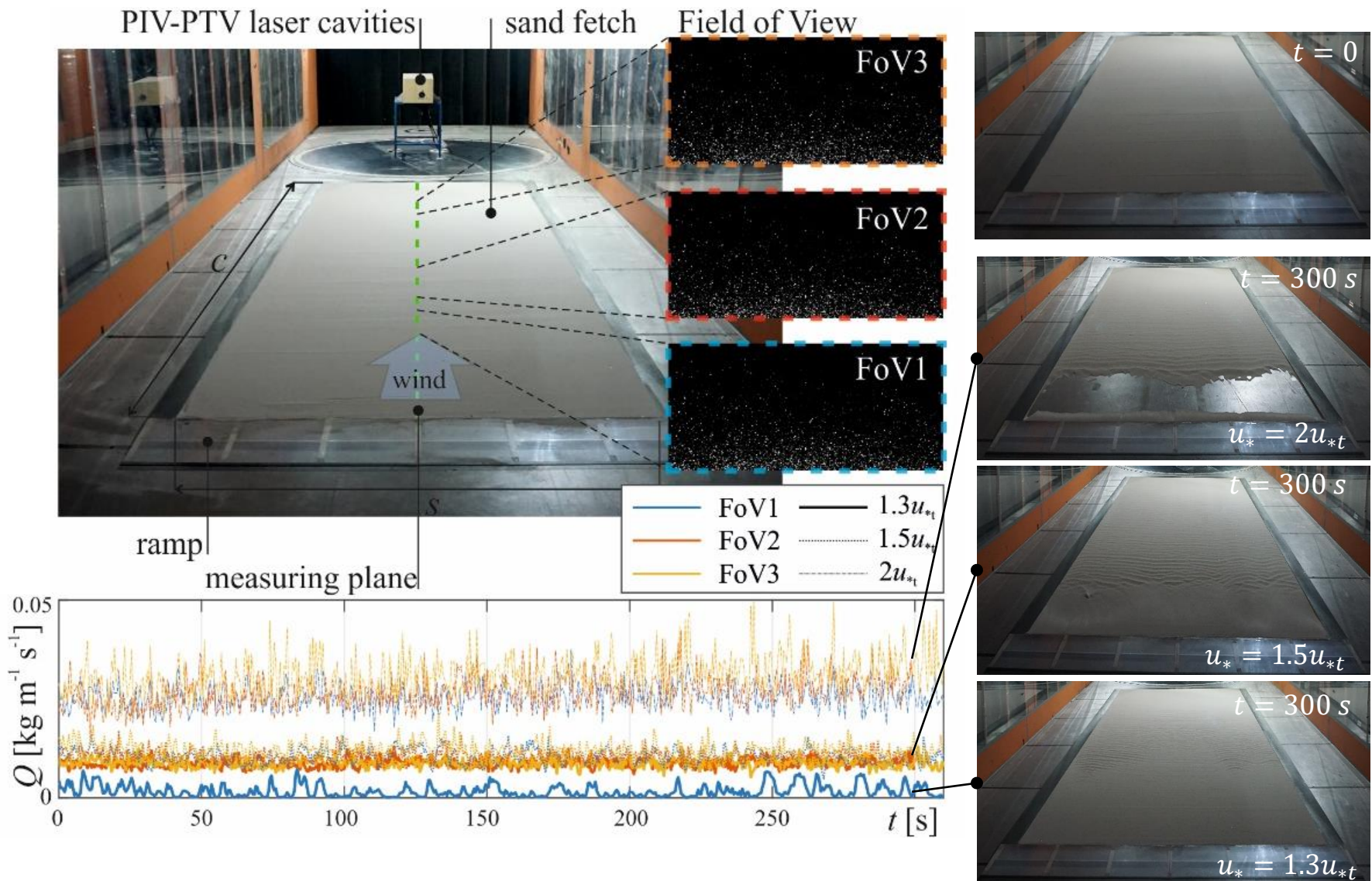


$\hookrightarrow$

<u>Sedimentation rate</u>	$f(Q_s) = C_s f(Q_{in})$
<u>Outgoing transport rate</u>	$f(Q_{out}) = [1 - C_s] f(Q_{in})$

# Wind-Sand Tunnel Testing: flat sand bed

1  
2  
3

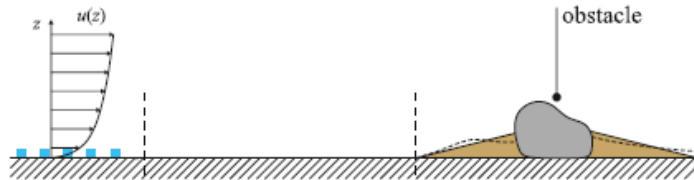


# Wind-Sand Tunnel Testing: obstacle

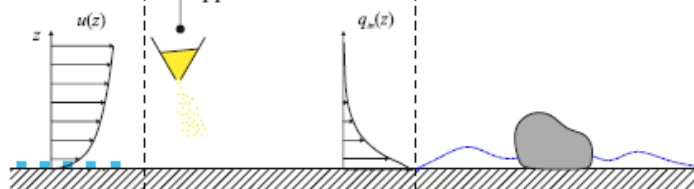
- State-of-the-art

1  
2  
3

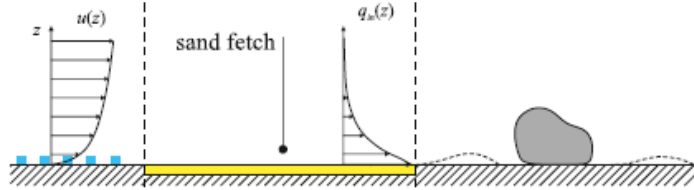
Setup A



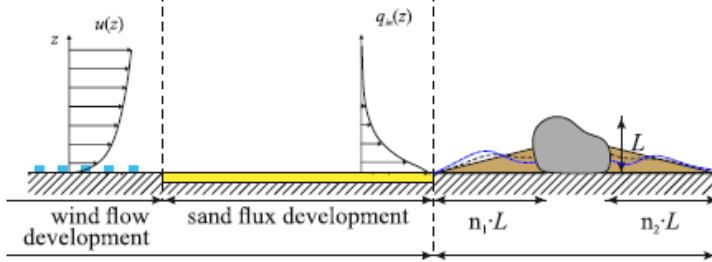
Setup B



Setup C

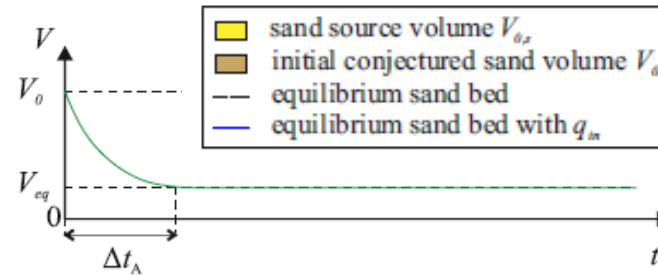


Setup D

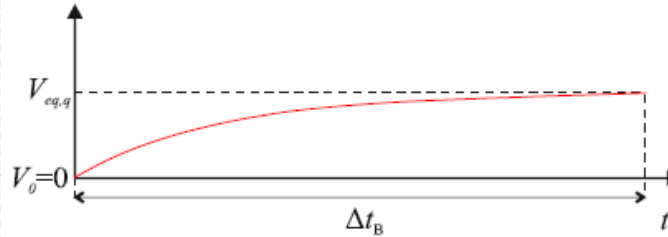


inlet section

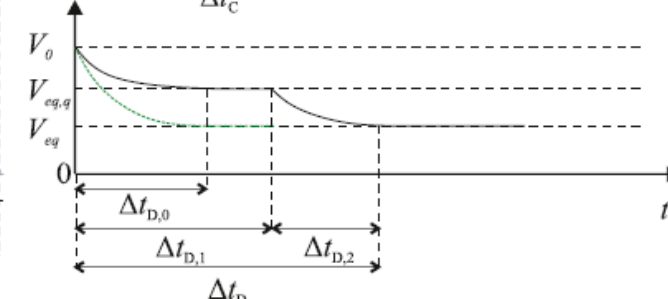
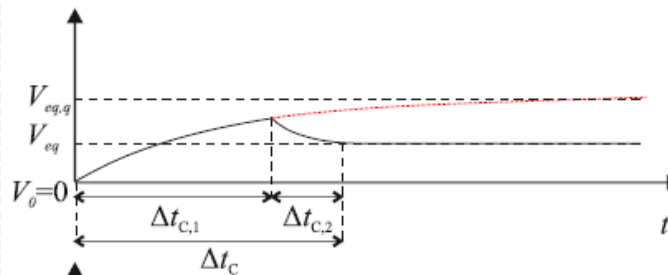
test section



Identification erosion/  
sedimentation zones



Sand transport and  
sedimentation regions  
around clean obstacle



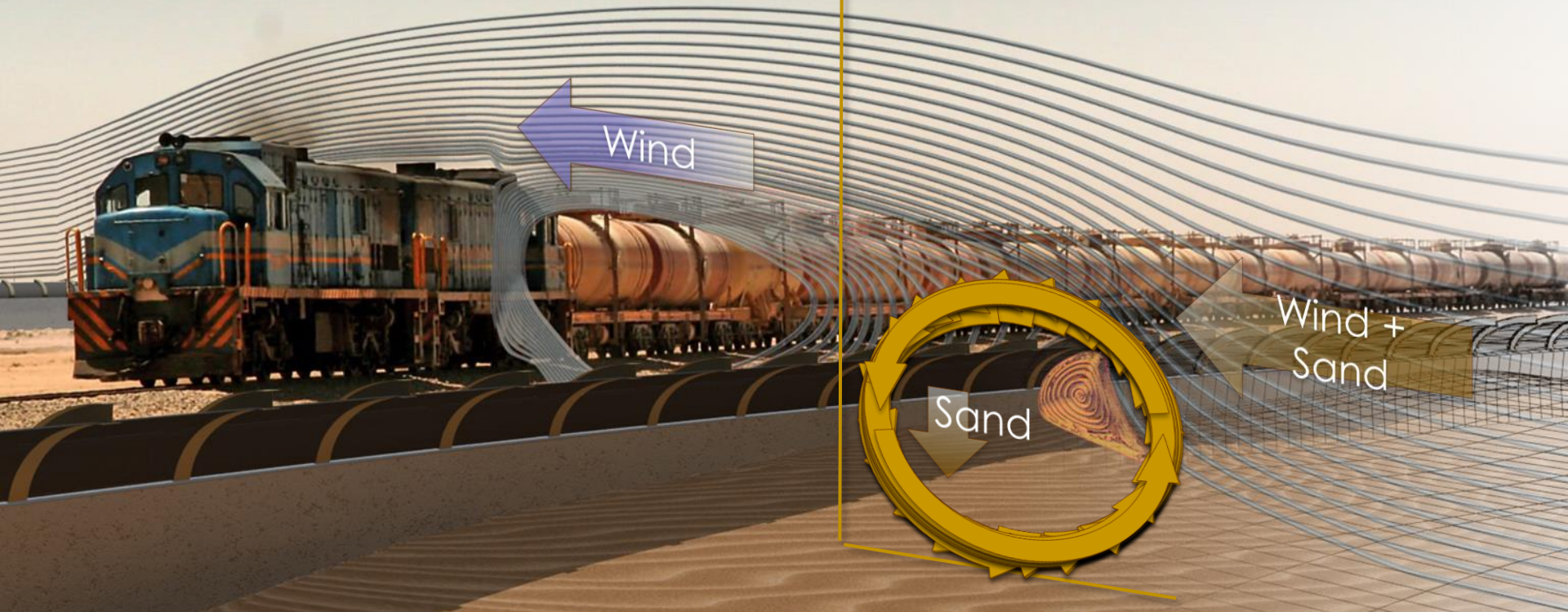
SMM performance  
assessment



# Wind-Sand Tunnel Testing: s4s



1. Trapping vortex
2. Reversed flow close to the ground
3. Sand subtraction from the incoming flux





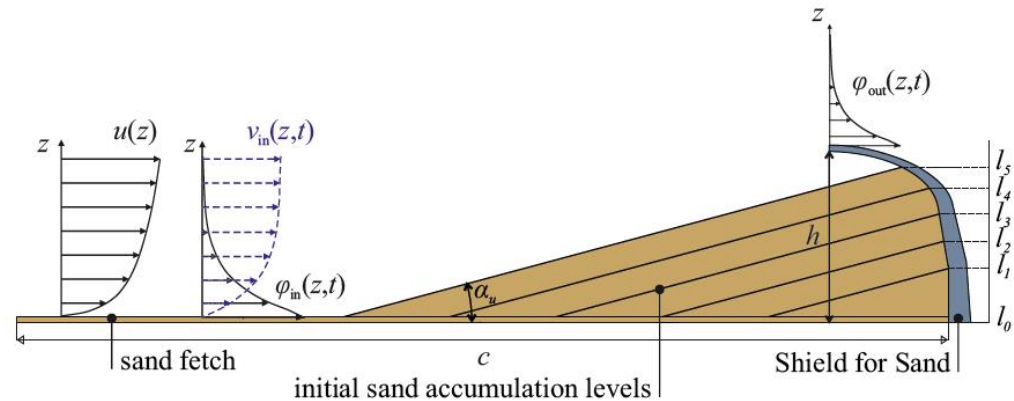
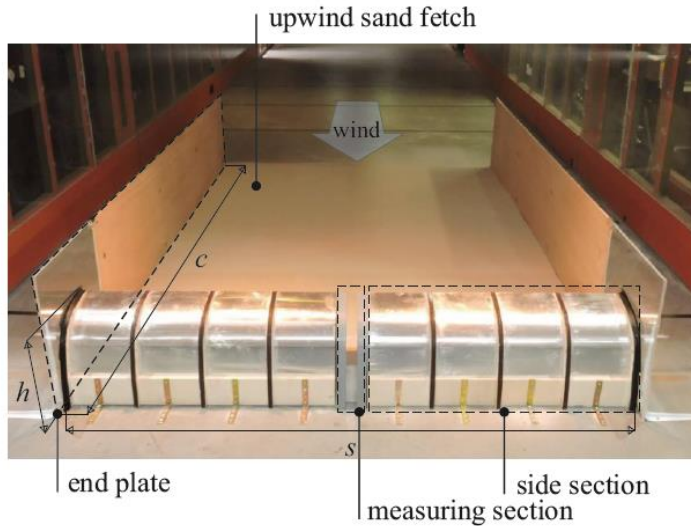
# Wind-Sand Tunnel Testing: s4s

1

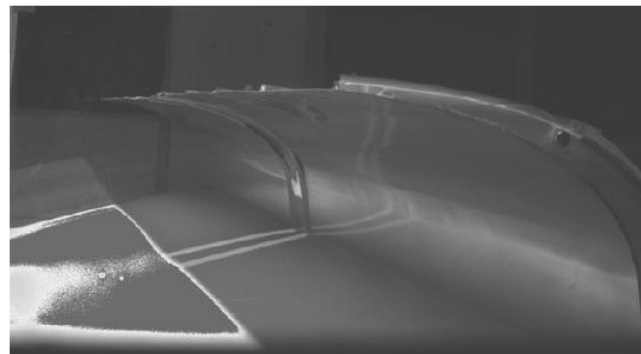
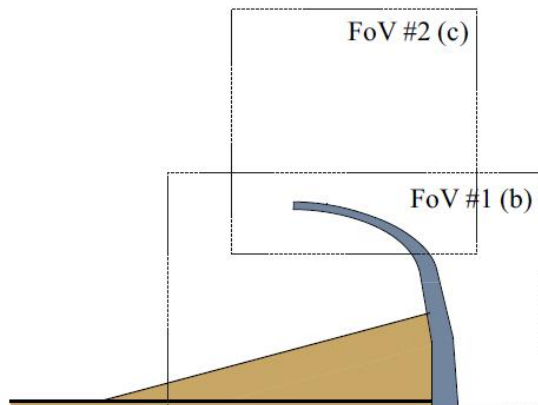
2

3

- Wind tunnel setup in L-1B



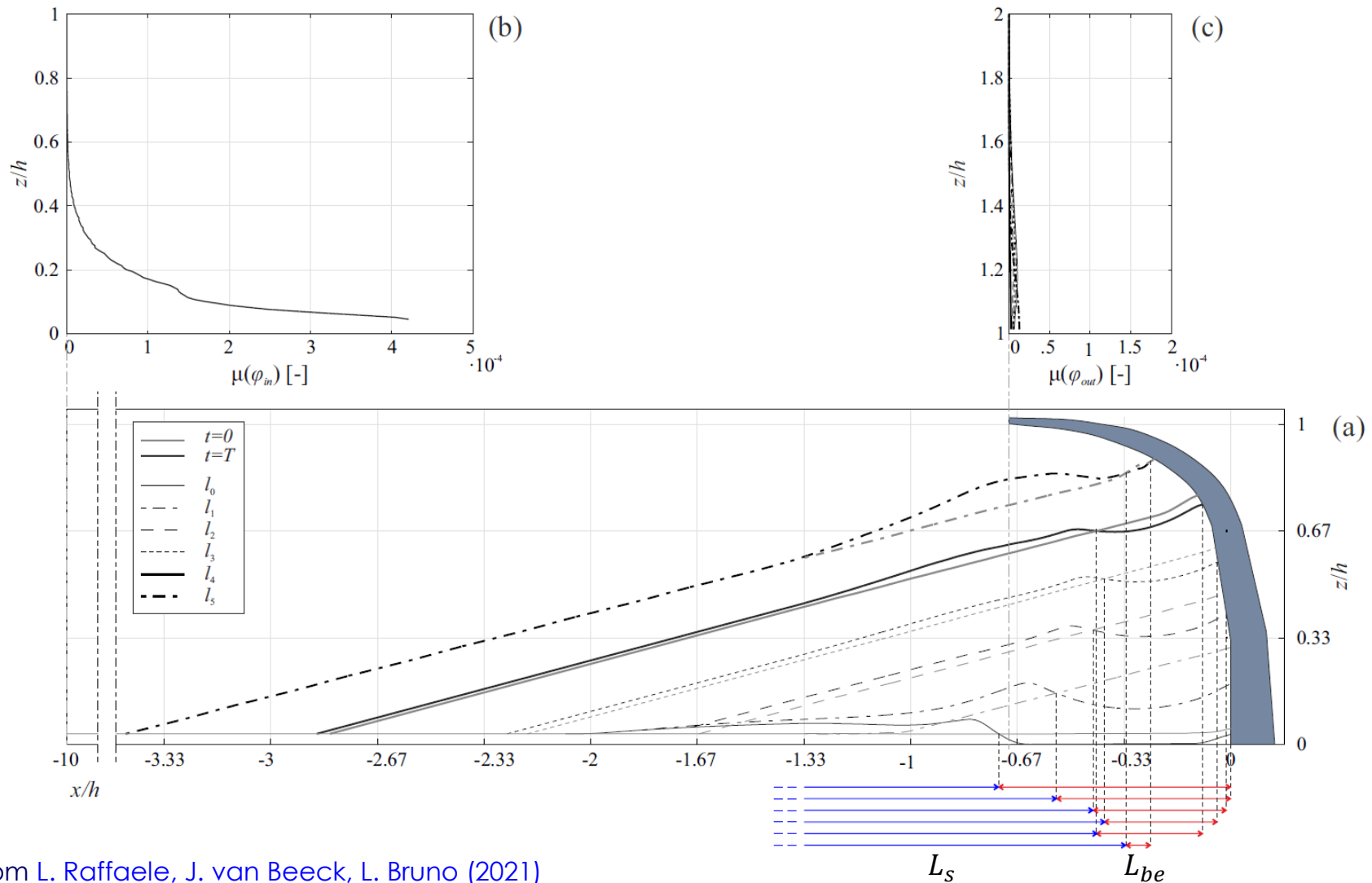
- PIV-PTV measurement setup



# Wind-Sand Tunnel Testing: s4s

1  
2  
3

- Sand concentration and morphodynamics



from L. Raffaele, J. van Beeck, L. Bruno (2021)

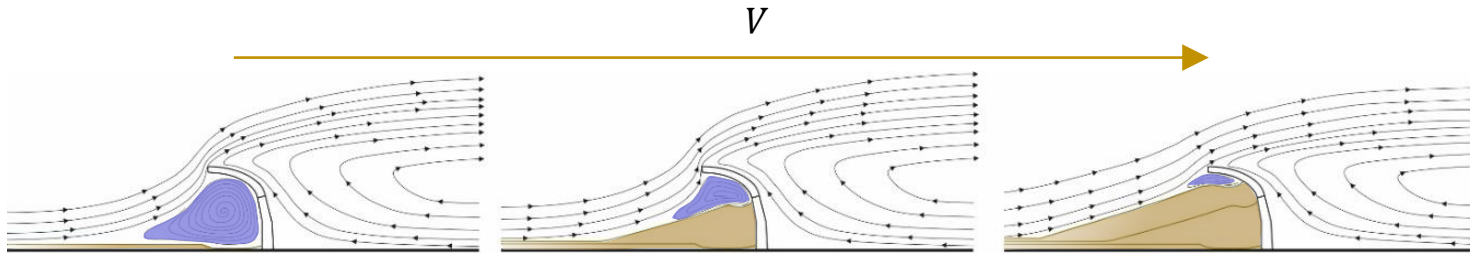
# Wind-Sand Tunnel Testing: s4s

1

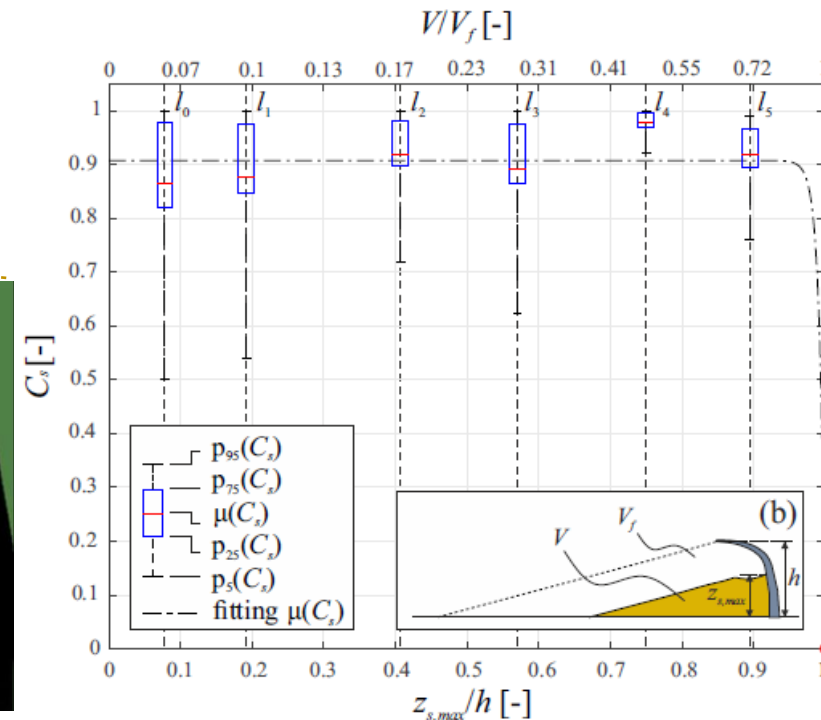
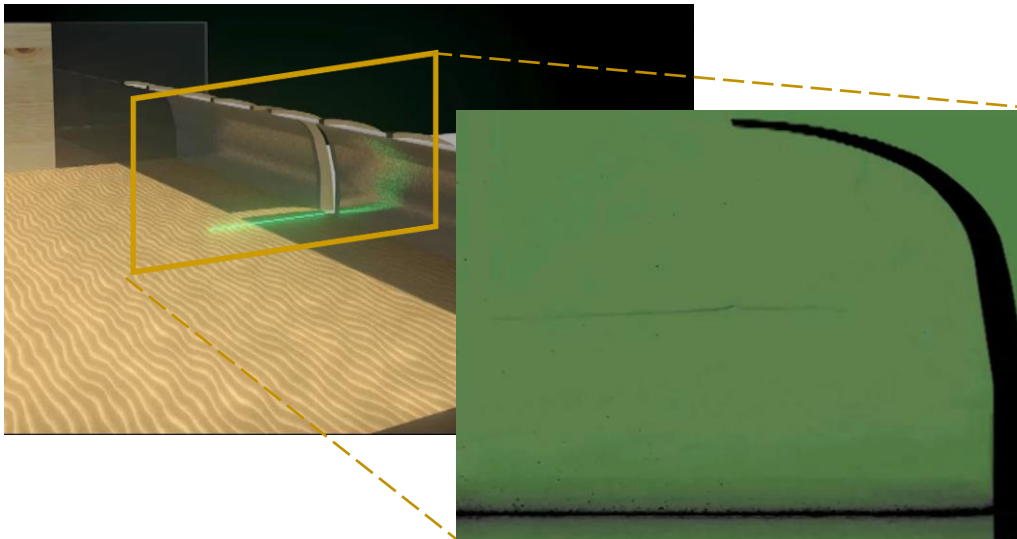
2

3

- Wind flow & morphodynamics pattern



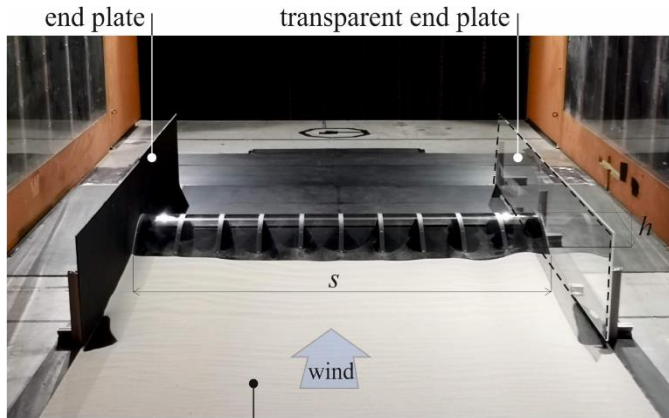
- Sedimentation Coefficient



# Wind-Sand Tunnel Testing: sinusoidal berm

1  
2  
3

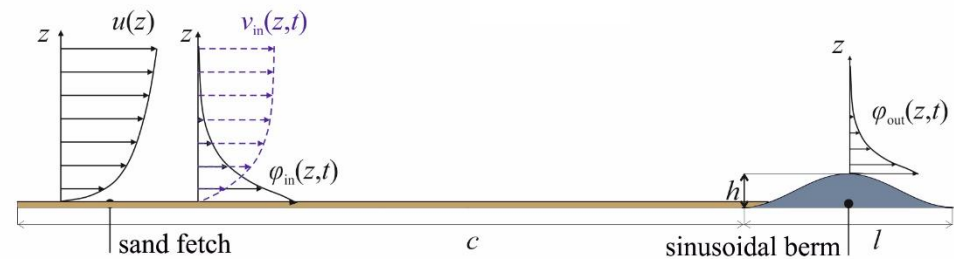
- Wind tunnel setup in L-1B



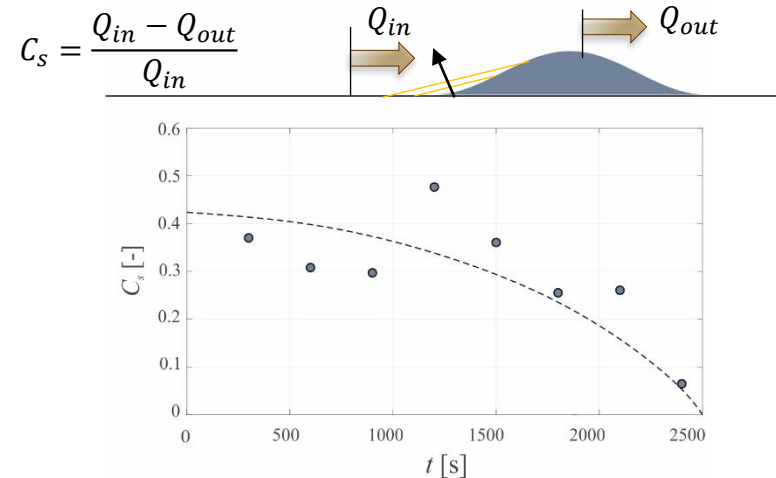
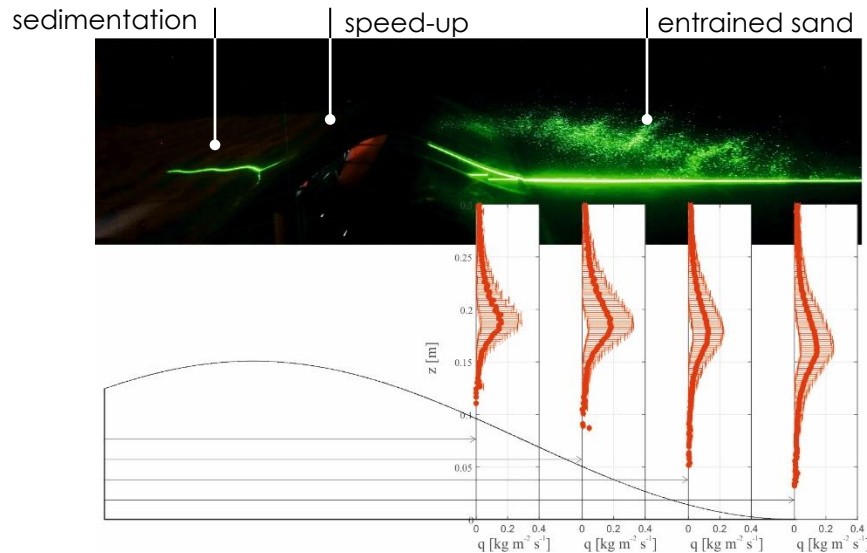
coast in Belgium



Mecca-Medina line



- Some results

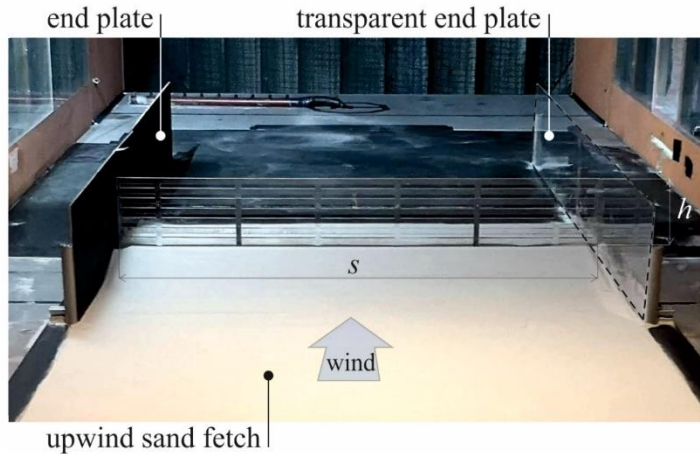




# Wind-Sand Tunnel Testing: porous fence

1  
2  
3

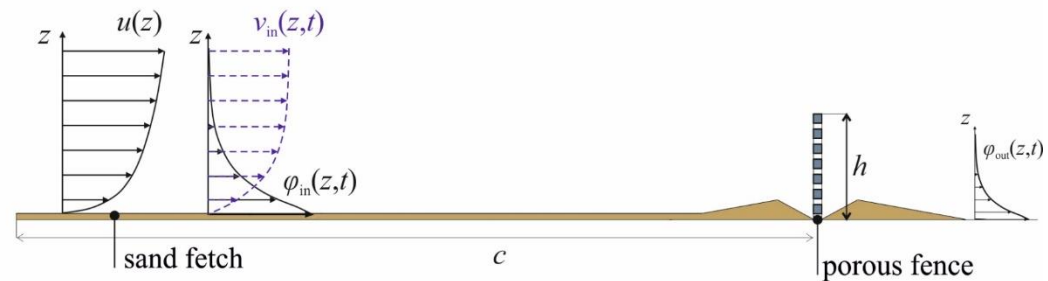
- Wind tunnel setup in L-1B



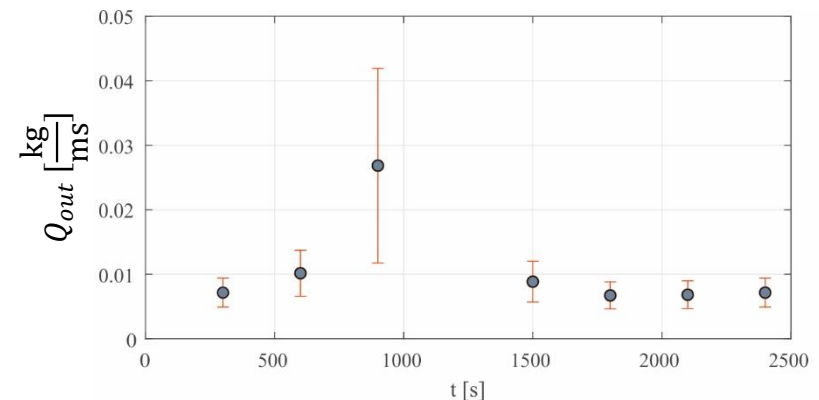
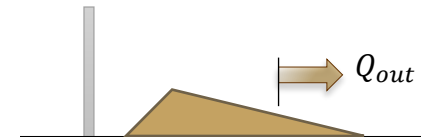
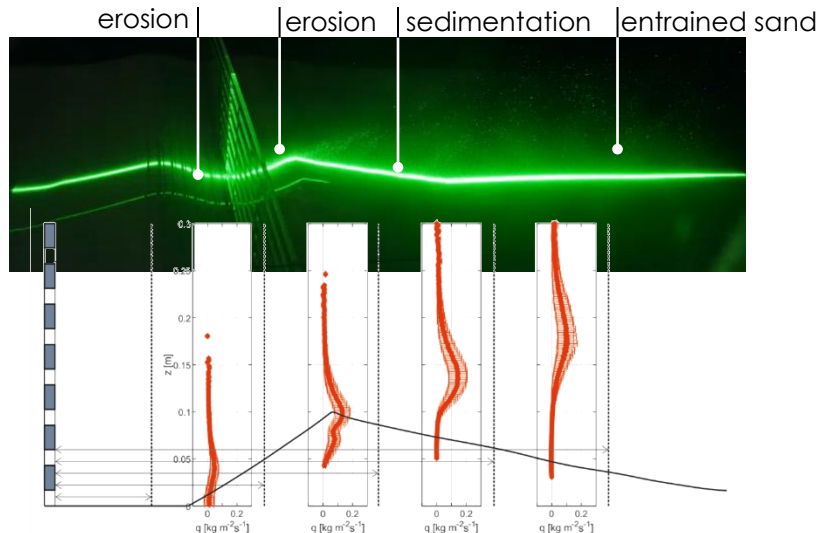
coast in Germany



railway in China

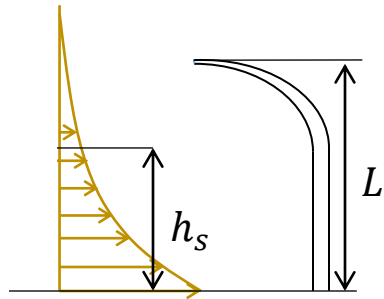


- Some results



# Similarity mismatching

- Similarity requirements VS past studies

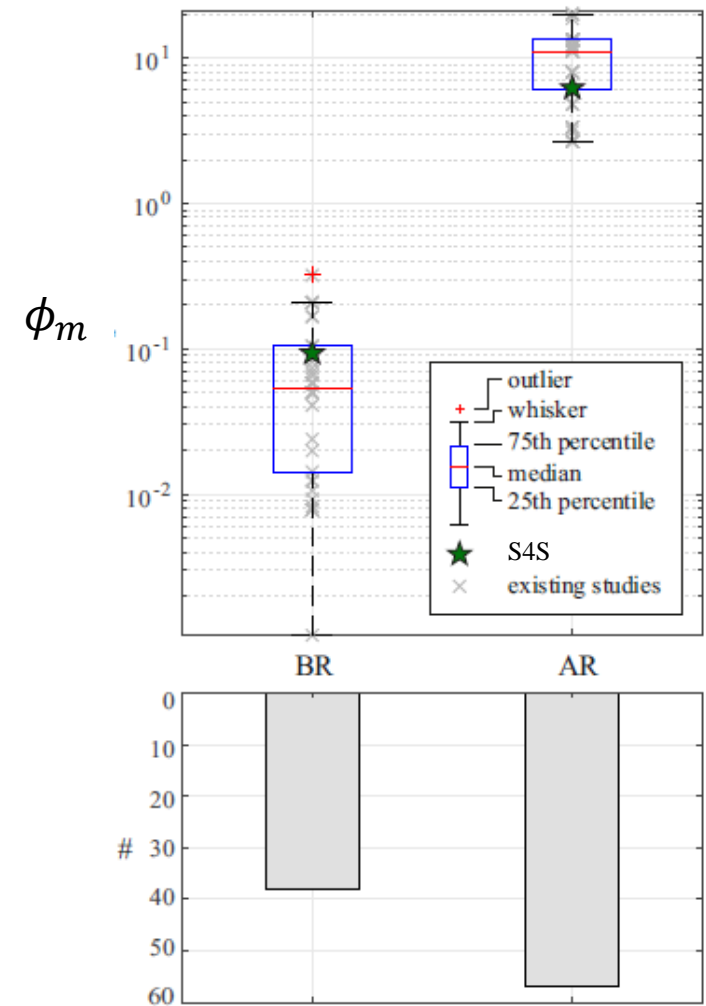
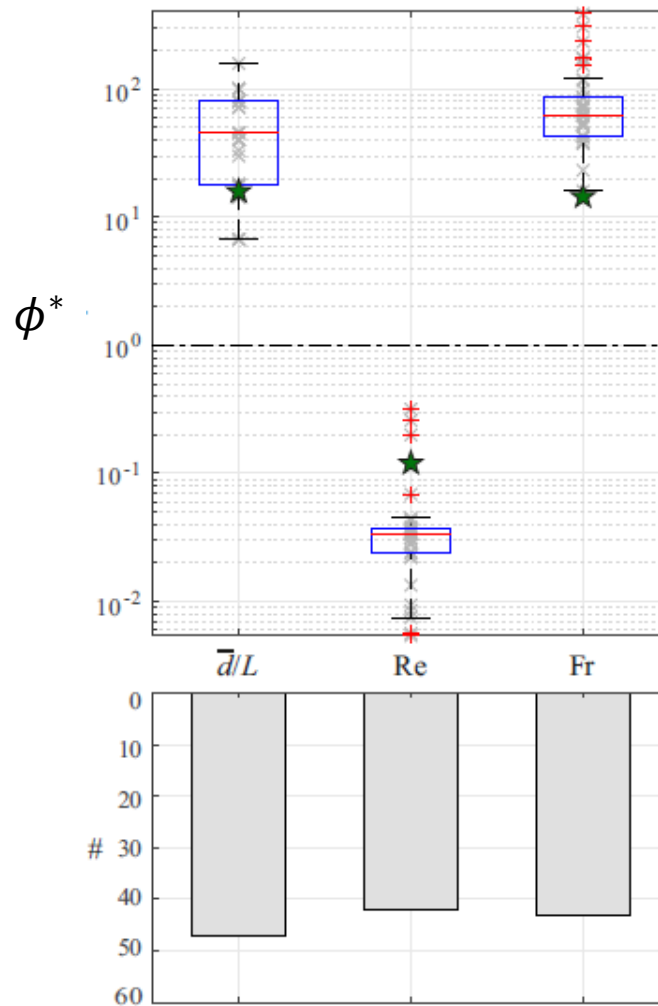


$$\left(\frac{L}{h_s}\right)_m \gg 1$$

$$\left(\frac{u_*}{u_{*t}}\right)_m = \left(\frac{u_*}{u_{*t}}\right)_p$$

$$\phi^* = \frac{\phi_m}{\phi_p}$$

$$\phi = \left\{ \frac{\bar{d}}{L}, Re, Fr \right\}$$



from L. Raffaele, J. van Beeck, L. Bruno (2021)

# Wind-Sand CFD model

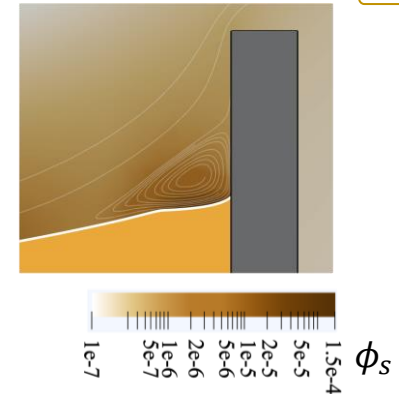
1  
2  
3

- Eulerian 1st order multiphase model

**Wind flow:**

RANS k- $\omega$  SST

$$\begin{cases} \nabla \cdot \bar{\mathbf{u}}_f = 0, \\ \frac{\partial \bar{\mathbf{u}}_f}{\partial t} + \bar{\mathbf{u}}_f \cdot \nabla \bar{\mathbf{u}}_f = -\frac{1}{\hat{\rho}_f} \nabla \bar{p} + \nabla \cdot \left[ (\nu_f + \nu_t) \nabla \bar{\mathbf{u}}_f \right], \\ \frac{\partial k}{\partial t} + \nabla \cdot (k \bar{\mathbf{u}}_f) = \nabla \cdot [(\sigma_k \nu_f + \nu) \nabla k] + \tilde{P}_k - \beta^* k \omega, \\ \frac{\partial \omega}{\partial t} + \nabla \cdot (\omega \bar{\mathbf{u}}_f) = \nabla \cdot [(\sigma_\omega \nu_f + \nu) \nabla \omega] + \alpha \frac{\omega}{k} P_k - \beta \omega^2 + (1 - F_1) \frac{2\sigma_\omega}{\omega} \nabla k \cdot \nabla \omega, \end{cases}$$



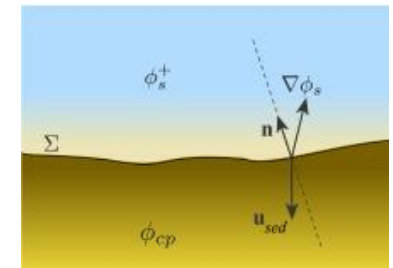
**Sand phase:**

Sand mass  
conservation equation

$$\begin{cases} \frac{\partial \phi_s}{\partial t} + \nabla \cdot \mathbf{q} = 0 \\ \mathbf{q} = \mathbf{u}_{tr} \phi_s + \mathbf{u}_{sed} \phi_s - \nu_{eff} \phi_s^{k-1} \nabla \phi_s \end{cases}$$

Sand erosion B.C.

$$-\nu_{eff} \phi_s^{k-1} \nabla \phi_s \cdot \mathbf{n} = A_H \hat{\rho}_f \sqrt{\frac{d}{g}} (u_*^2 - u_{*t}^2)_+ \quad \text{Ho et al. (2012)}$$



Sand bed  
morphodynamic evolution

$$v_{\Sigma}^{ED} \cdot \mathbf{n} = -\frac{1}{\phi_{cp} - \phi_s} \mathbf{q} \cdot \mathbf{n} = \underbrace{\frac{\phi_s (\mathbf{u}_{tr} + \mathbf{u}_{sed}) \cdot \mathbf{n}}{\phi_{cp} - \phi_s}}_{\text{Deposition}} + \underbrace{\frac{\nu_{eff} \phi_s^{k-1} \nabla \phi_s \cdot \mathbf{n}}{\phi_{cp} - \phi_s}}_{\text{Erosion}}$$

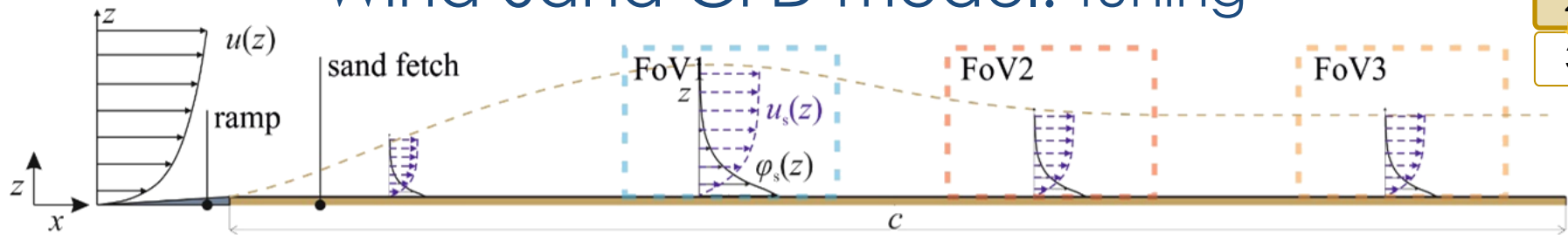
Sand avalanching

$$\frac{\partial h}{\partial t} = \nu_{av} \nabla \cdot \left[ \frac{(|\nabla h| - \tan \theta_{cr})_+}{\sqrt{1 + |\nabla h|^2}} \frac{\nabla h}{|\nabla h|} \right] + \text{Deposition} + \text{Erosion}$$

Lo Giudice and Preziosi, Appl. Math. Model. (2020)



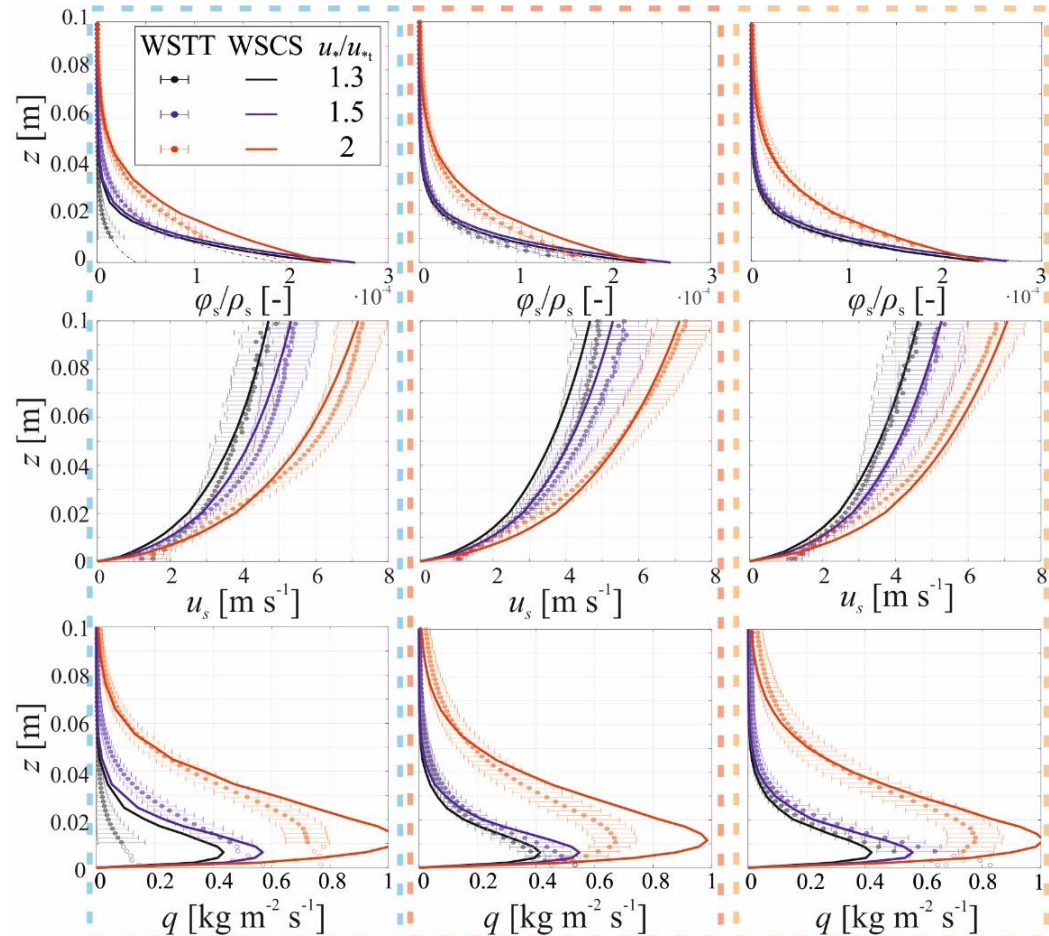
# Wind-Sand CFD model: tuning



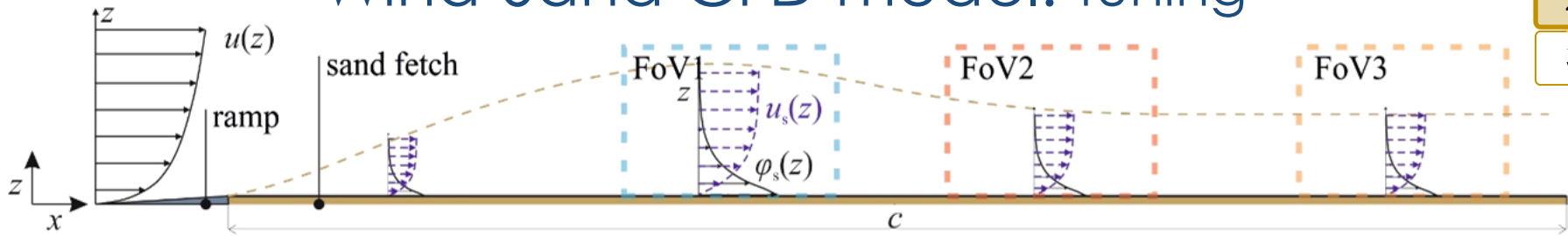
Mean sand concentration  $\phi_s$

Mean sand velocity  $u_s$

Mean sand flux  $q$

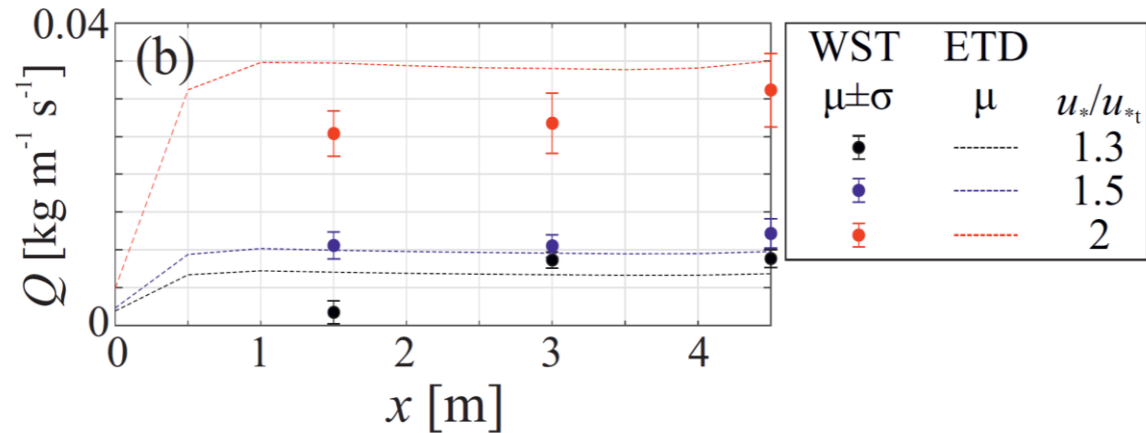


# Wind-Sand CFD model: tuning



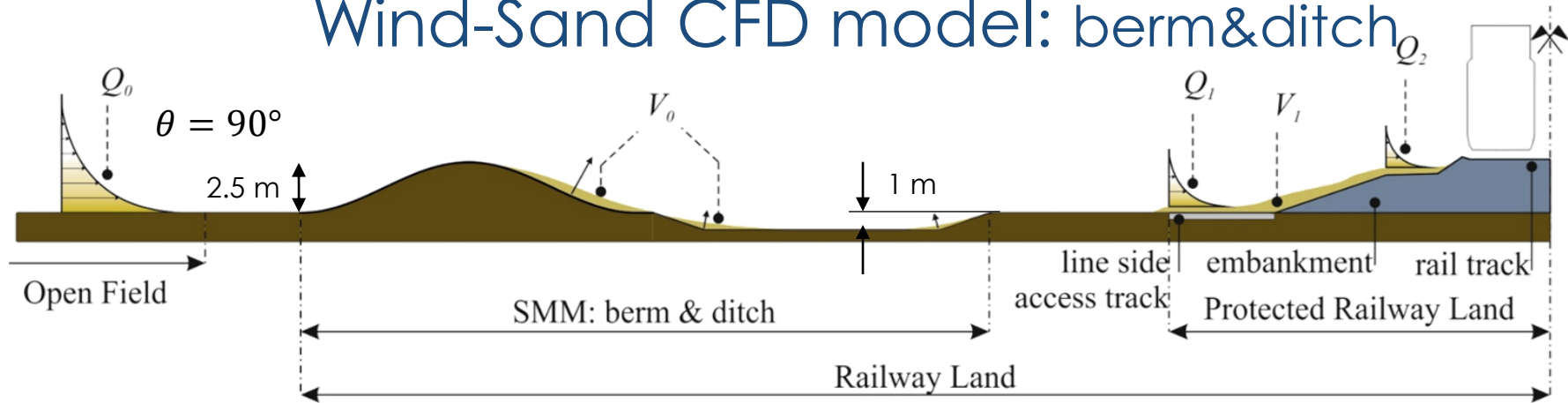
sand transport rate

$$Q = \int_0^{+\infty} q(z) dz$$



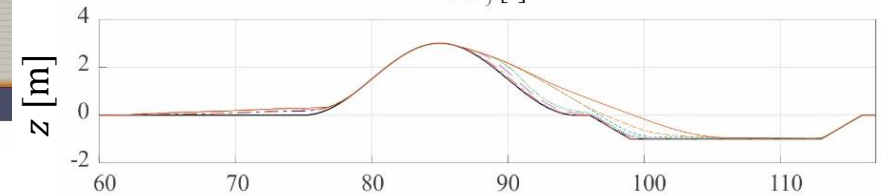
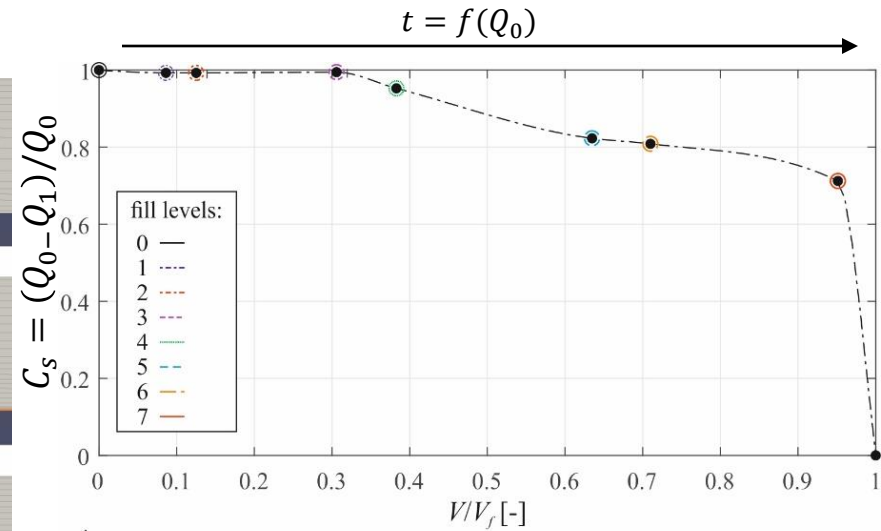
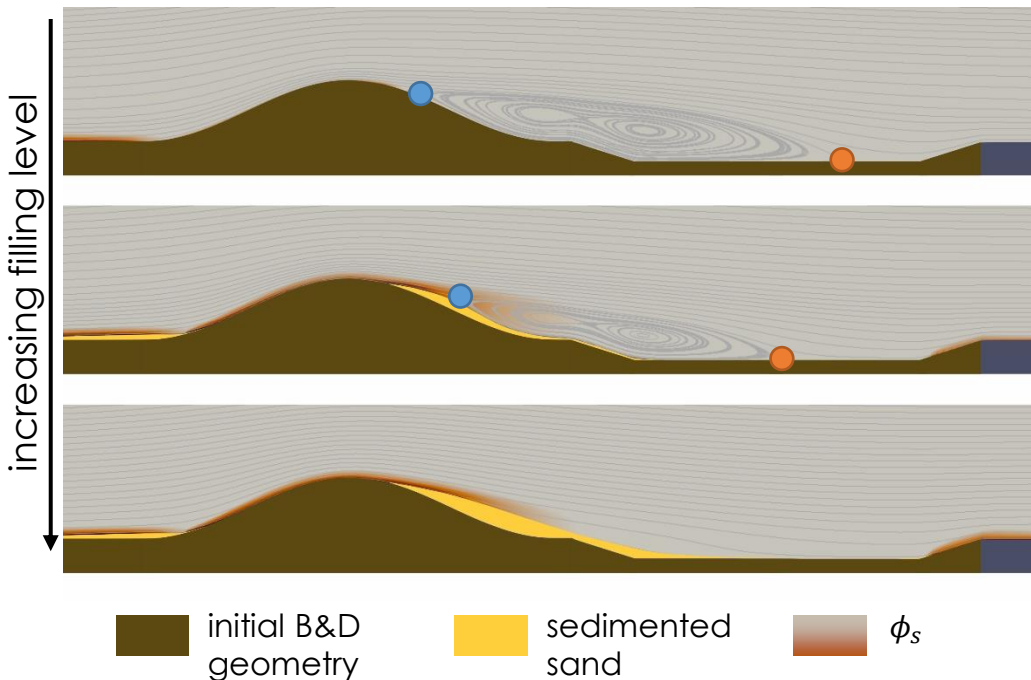
- WSTs results are reproduced fairly good
- Mismatching of experimental results induced by:
  - (i) high intermittency for  $u_*/u_{*t} = 1.3$
  - (ii) short fetch length
  - (iii) 1<sup>st</sup> order nature of the model

# Wind-Sand CFD model: berm&ditch



- 1
- 2
- 3

## SMM aerodynamic working principle



from L. Raffaele, N. Coste, G. Glabeke (2022)



# Windblown sand action

1  
2  
3

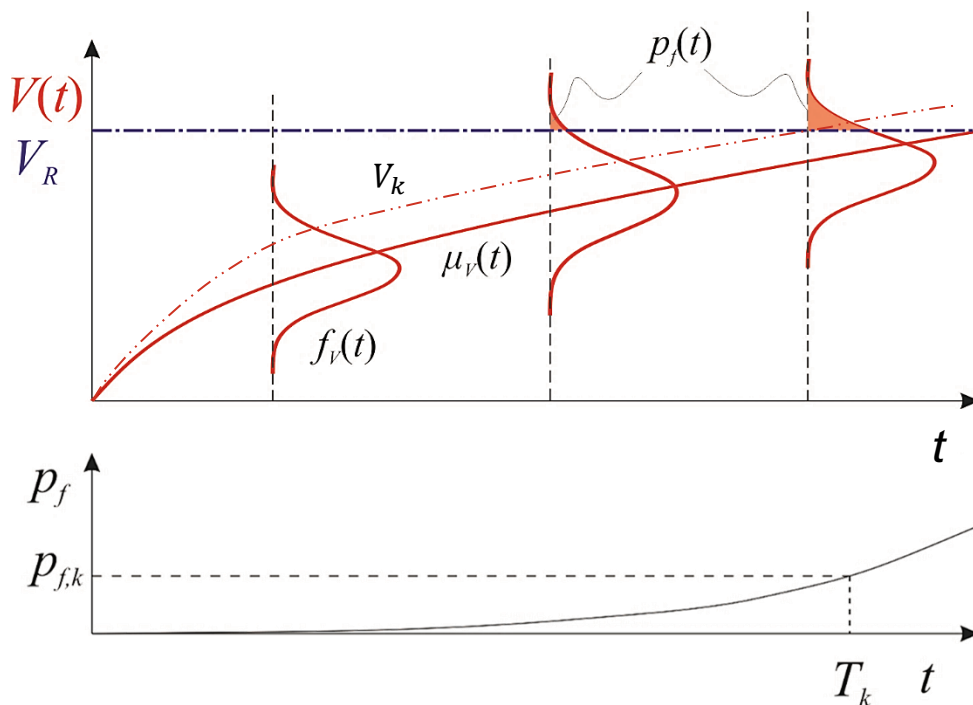
Time-variant WbS action  $V(t)$

$$f_V(t) = \sum_{n=1}^{\infty} (g_1 * g_i * \dots * g_n) C_s Q_{in} P[N_{\theta} = n]$$

Resistant sand volume  $V_R$

- Structure/Infrastructure  $\leftarrow$  **SLS**
- SMM  $\leftarrow$  efficiency ( $C_s$ )

**Time variant reliability analysis**  $V(t) < V_R$



Probability of failure

$$p_f(t) = P[V(t) \geq V_R]$$

$$= \int_0^{+\infty} F_{V_R}(x) f_V(x, t) dx = 1 - F_V(V_R, t)$$

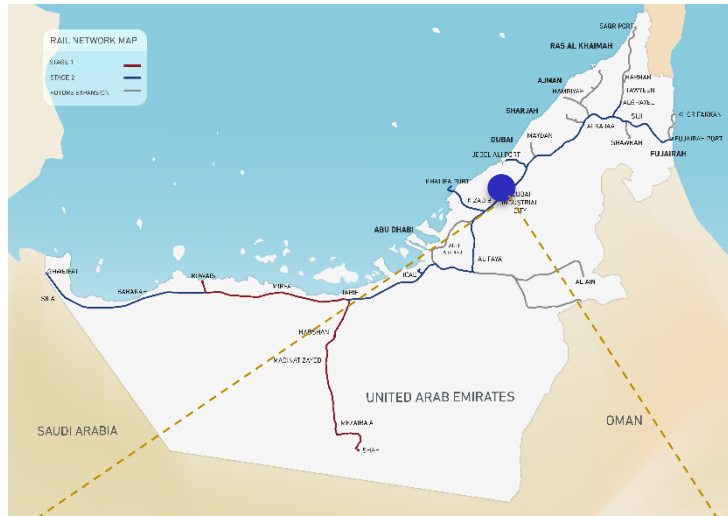
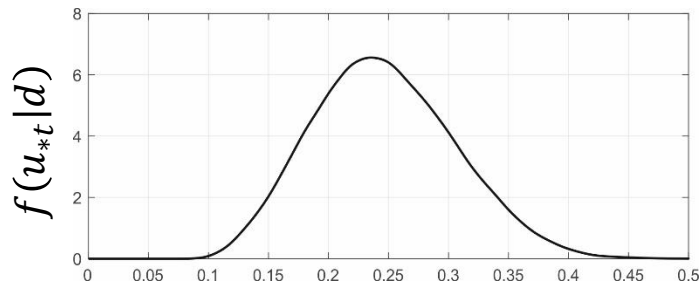
Characteristic time of failure

$$T_k = p_f^{-1}(p_{f,k}) \quad \text{e.g. } p_{f,k} = 5\%$$

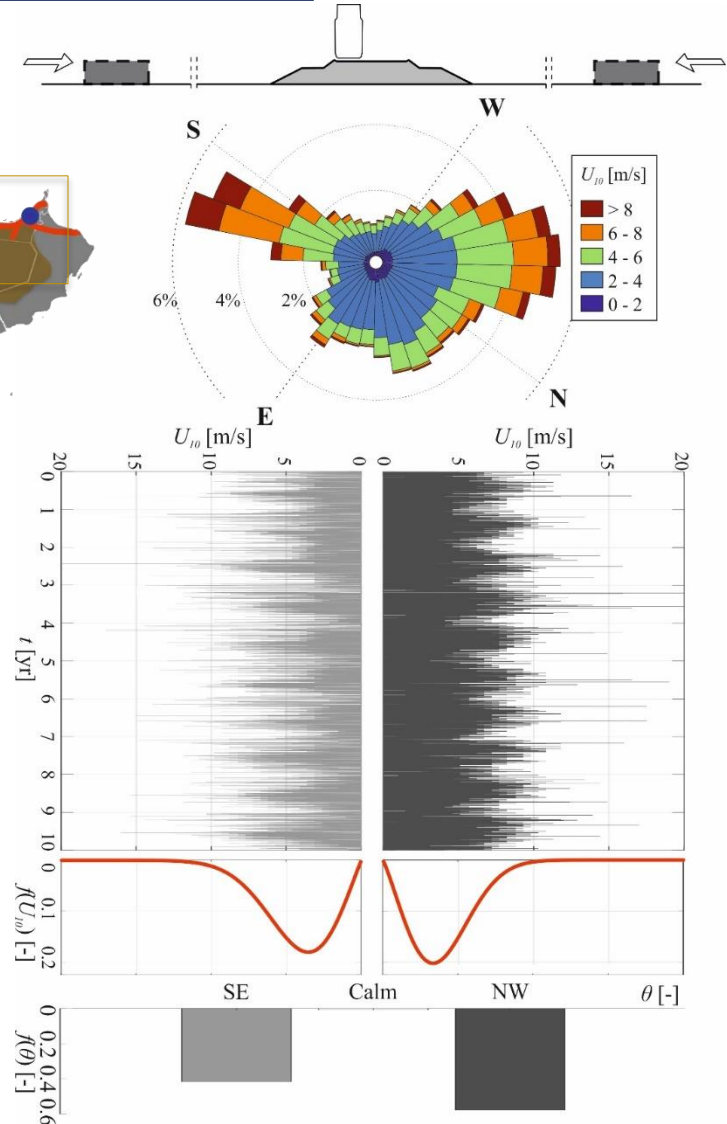


sand removal period  $\leq T_k$

## A case study: wind-sand site analysis

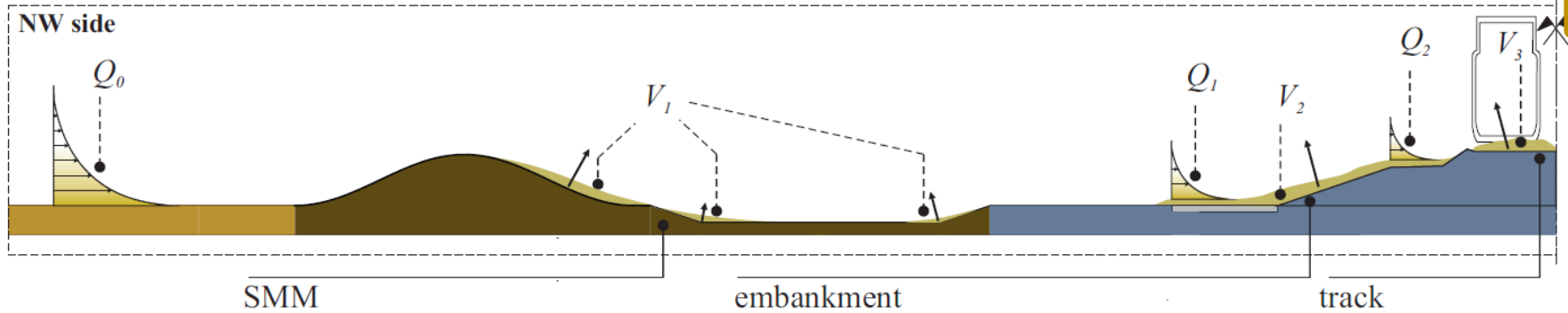
 $u_{*t}$  statistics ( $d = 0.147$  mm) $u_{*t}$  from Raffaele et al (2016)

Wind statistics  $z_0 = 4e - 3 \text{ m}$

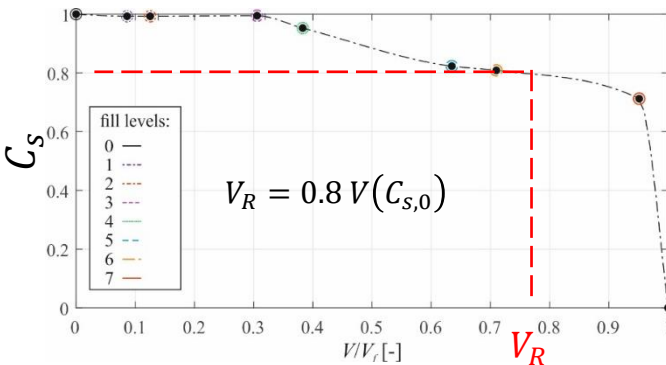


# A case study: sedimentation coeffs

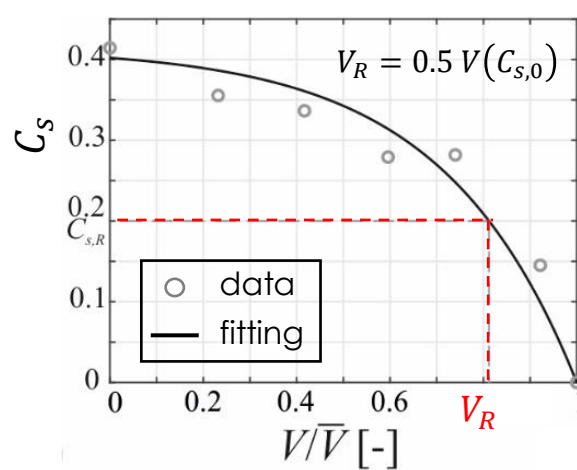
1  
2  
3



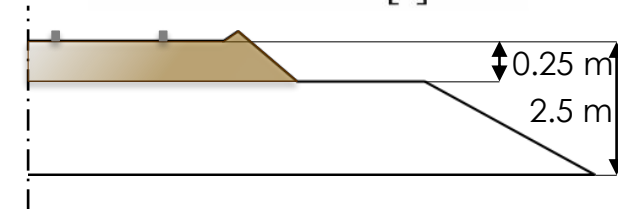
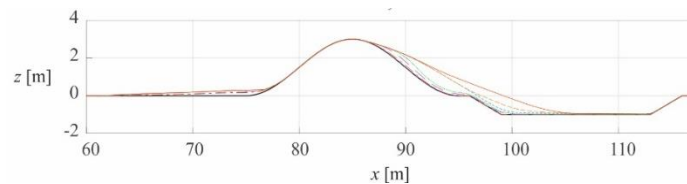
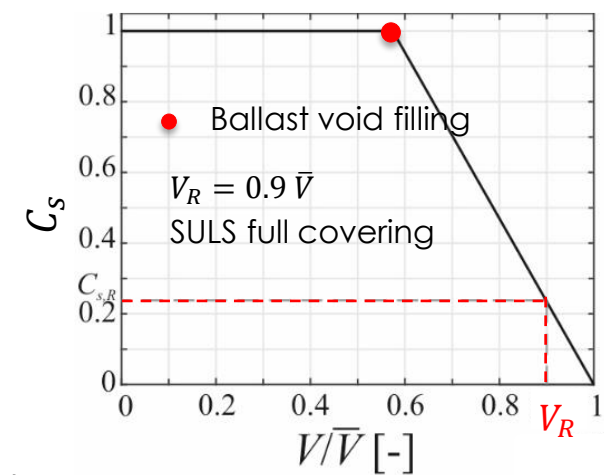
from WT+CFD Raffaele et al. (2022)



from WT tests Hotta & Horikawa (1990)



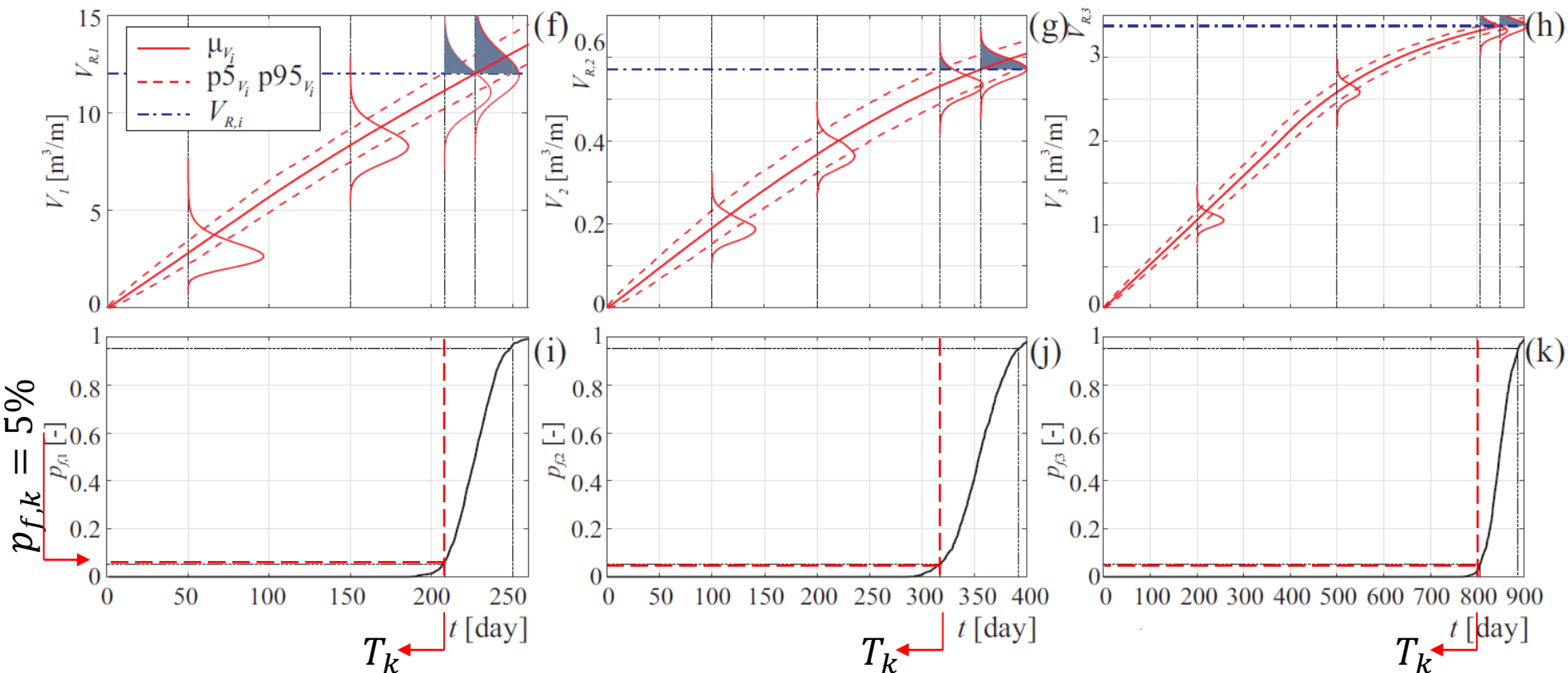
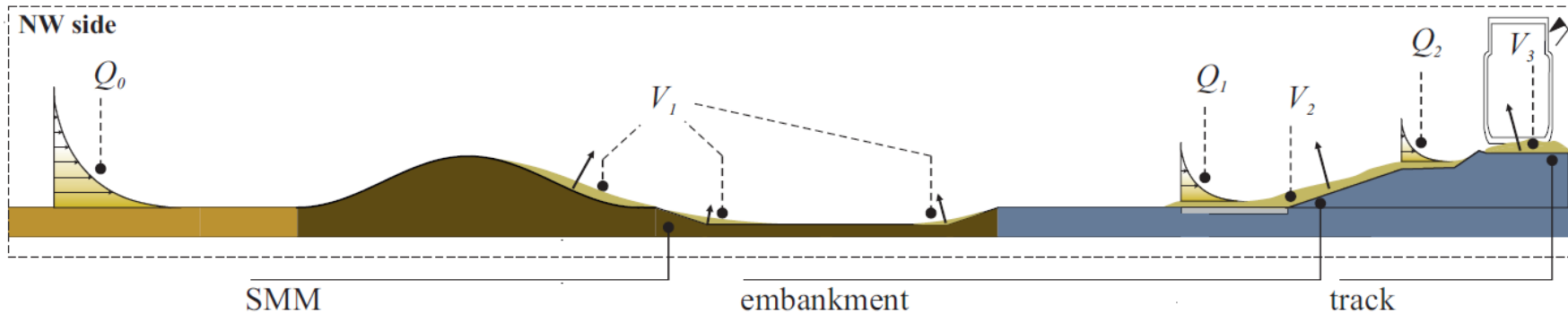
conjectured





# A case study: windblown sand action (NW)

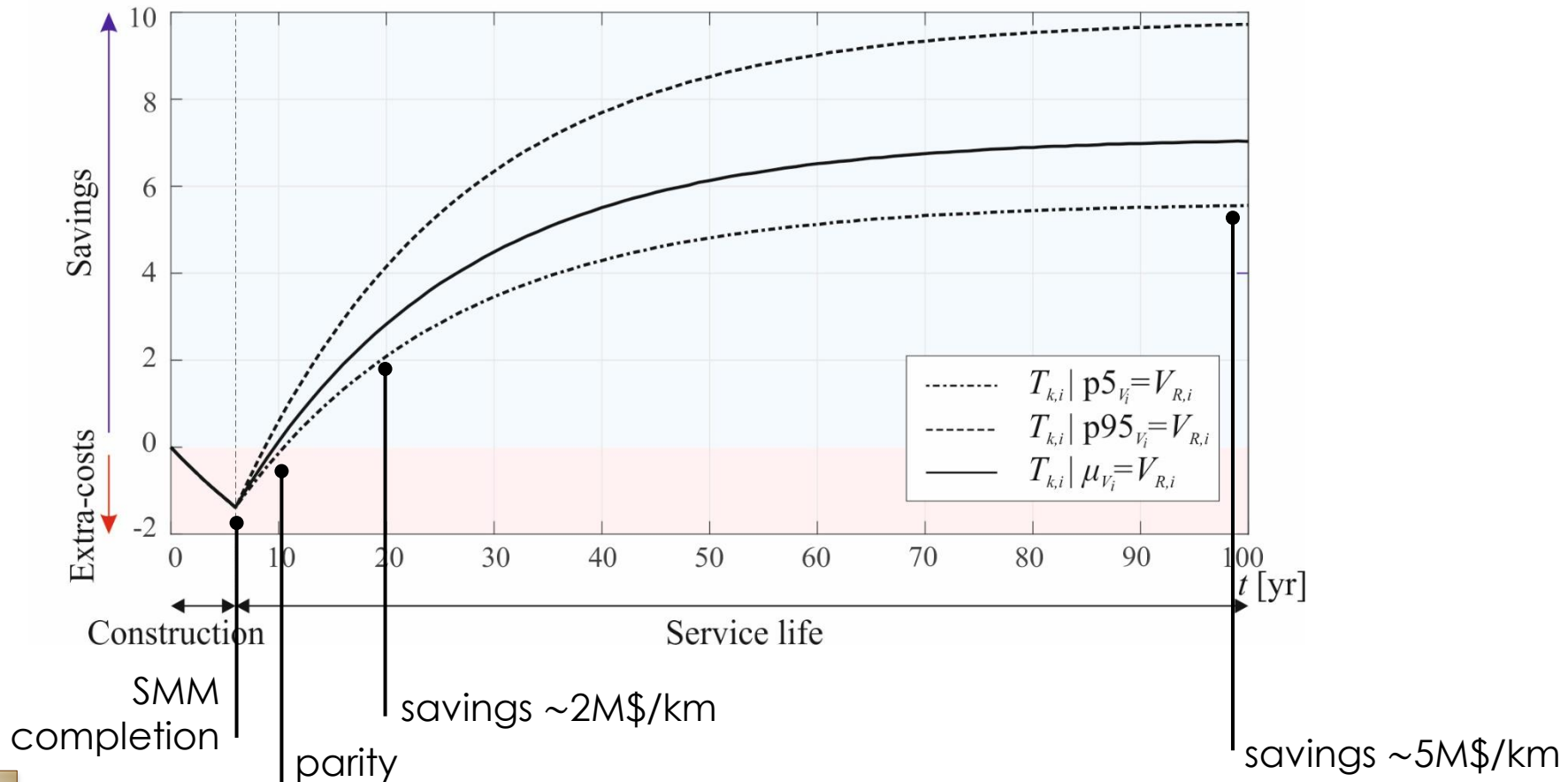
1  
2  
3



# A case study: LCCA

$$c(t_L) = \sum_{t=1}^{t_L} \left[ \frac{c_d/T_d + \sum_{i=1}^N c_{s,i}/T_{k,i}}{(1+r)^t} \right] \Rightarrow \Delta c = c(t_L)_{SMM} - c(t_L)_0$$

$\Delta c$  [M\$/km]



cumulated savings are impressive w.r.t. railway avg worth (in ME ~4M\$/km)

# To sum up

The proposed modelling framework allows to:

- Move from trial-and-error to rationale design
- Assess the performances of SMMs
- Plan sand removal maintenance operations
- Assess the economic impact of SMMs

## Next steps...

- Validation of Wind-Sand CFD model thanks to wind tunnel testing
- Quantification of scale effect induced by wind tunnel scaling by means of Wind-Sand CFD simulations





## Hybrid Performance assessment of Sand Mitigation Measures



EU Horizon 2020 Marie Curie Individual Fellowship



von KÁRMÁN INSTITUTE  
FOR FLUID DYNAMICS



OPTIFLOW

WSMM

HyPer SMM received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 885985